## Electronic Supplementary Material to: Relationships between Cloud Droplet Spectral Relative Dispersion and Entrainment Rate and Their Impacting Factors\*

Shi LUO<sup>1,2</sup>, Chunsong LU<sup>2</sup>, Yangang LIU<sup>3</sup>, Yaohui LI<sup>1</sup>, Wenhua GAO<sup>4</sup>, Yujun QIU<sup>2</sup>, Xiaoqi XU<sup>5</sup>, Junjun LI<sup>2</sup>, Lei ZHU<sup>2</sup>, Yuan WANG<sup>6</sup>, Junjie WU<sup>1</sup>, and Xinlin YANG<sup>1</sup>

<sup>1</sup>College of Aviation Meteorology, Civil Aviation Flight University of China, Guanghan 618307, China

<sup>2</sup>Collaborative Innovation Center on Forecast and Evaluation of Meteorological Disasters (CIC-FEMD)/

Key Laboratory for Aerosol-Cloud-Precipitation of China Meteorological Administration,

Nanjing University of Information Science & Technology, Nanjing 210044, China

<sup>3</sup>Environmental and Climate Sciences Department, Brookhaven National Laboratory, Upton, New York 11973, US

<sup>4</sup>State Key Laboratory of Severe Weather, Chinese Academy of Meteorological Sciences, Beijing 100081, China <sup>5</sup>Nanjing Joint Institute for Atmospheric Sciences, Nanjing 210019, China

<sup>6</sup>Collaborative Innovation Center for Western Ecological Safety, Lanzhou University, Lanzhou 730000, China

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**Fig. S1.** The initial CDSD with initial liquid water content (LWC<sub>i</sub>) of 0.5 g m<sup>-3</sup>, initial droplet number concentration ( $n_i$ ) of 119.4 cm<sup>-3</sup>, initial mean volume radius ( $r_{vi}$ ) of 10 µm, shape parameter ( $\mu$ ) of 40.0, and relative dispersion (d) of 0.16.

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Fig. S2. The relationship of entrainment rate ( $\lambda$ ) and entrained environmental air blob numbers of the second entrainment-mixing process ( $N_2$ ).



**Fig. S3.** Temporal evolution of cloud droplet spectral relative dispersion (*d*) with the entrained environmental air blob number of the first entrainment-mixing process ( $N_1$ ) equal to 2, 4, 6, 8, and 10.



**Fig. S4.** Temporal evolutions of cloud droplet size distribution for entrained environmental air blob numbers of the second entrainment-mixing process ( $N_2$ ) equal to 2, 4, 6, 8, and 10. Left: entrained environmental air without cloud condensation nuclei (CCN). Right: entrained environmental air with CCN. The vertical magenta and black lines represent the ending and beginning time of the first and second entrainment-mixing processes, respectively. The horizontal line represents the criterion of small droplets. The first and second entrainment-mixing processes are labeled as "Mix 1" and "Mix 2", respectively, as well as "adiabatic" for the adiabatic ascending process.



**Fig. S5.** The cloud droplet size distributions just before and after the second mixing processes when the entrained environmental air blob number of the second entrainment-mixing process ( $N_2$ ) is equal to 2, 4, 6, 8, and 10. Left: entrained environmental air without cloud condensation nuclei (CCN). Right: entrained environmental air with CCN.



**Fig. S6.** Temporal evolutions of relative dispersion (a) and the ratio of (b) small droplet number concentration  $(n_s)$  to total droplet number concentration  $(n_c)$  for entrained blob size (l) equal to 1 m. The entrained environmental air blob numbers of the second entrainment-mixing process  $(N_2)$  equal 2, 4, 6, 8, and 10. The triangle and pentagram represent the ending of the first entrainment-mixing process and the beginning of the second entrainment-mixing process, respectively.