

# Local Similarity Relationships of Non-Dimensional Wind and Temperature Gradient in the Tower-Layer Atmosphere over Beijing City<sup>①</sup>

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## ABSTRACT

Micrometeorological data for wind and temperature from a 325 m high tower in Beijing City are analyzed by use of local similarity theory. Non-dimensional wind and temperature gradients,  $\Phi_w$  and  $\Phi_\theta$ , are determined by three techniques called, respectively, eddy-correlation, mean profiles and inertia-subrange cospectra (ISC) method for a wide range of atmospheric stratification from unstable to stable conditions. Average dissipation rate  $\Phi_\epsilon$  of turbulent kinetic energy (TKE) is evaluated from  $\nu$ -spectrum, as a quantity required in the last technique. Ratio of the eddy transfer coefficients,  $\chi (= K_h / K_m)$ , is calculated from  $\Phi_w$  and  $\Phi_\theta$  estimations. The results from various techniques are compared with each other and with some available empirical results in the tower-layer. It is shown that the empirical relationships determined by mean profiles and ISC methods in the tower-layer turbulence are in agreement with each other and with some other results.

**Key words:** Local similarity, Non-dimensional gradients of wind and temperature, Dissipation rate, Ratio of eddy diffusivities, Spectra and Cospectra

## 1. Introduction

The local similarity theory is one of the powerful tools of similarity theory in the analysis of turbulence flow in the atmospheric boundary layer (ABL). This theory provides a set of empirical relationships to describe the meteorological parameters in the tower-layer atmosphere. These relationships can be expressed as a function of stability parameter,  $\zeta_1 (= z / L_1)$ , where  $z$  is the height and  $L_1$  the local Monin-Obukhov length. Monin-Obukhov similarity has been applied to the surface layer (e.g. Monin and Obukhov, 1954; Businger et al., 1971), while local similarity theory is limited to the lower level of the ABL (e.g. Nieuwstadt, 1984; Sorbjan, 1986a,b; Zhang et al., 1991; Hu and Zhang, 1993; Xu et al., 1997; Al-Jiboori et al., 2000).

Most previous studies analyzed the turbulence characteristics in the tower-layer and pointed out that dimensionless standard deviations, gradient fluxes and dissipation rates for velocity and temperature variance are functions of  $\zeta_1$ . The local similarity proposed first by Nieuwstadt (1984) was applied to describing turbulence characteristics over meteorological mast in the stable boundary layer. Based on the data from the same tower used in the present study, Zhang et al. (1991) found that the dimensionless variable groups  $\sigma_i / u_{*1}$  are functions of  $(z / L_1)$  ( $i=1, 2, 3$ ) under unstable conditions. Xu et al. (1997) showed that the

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turbulence structure on meteorological towers in Nanjing City and its suburb could be ordered well by local similarity scales  $u_{*1}$ , space  $T_{*1}$ , space  $L_1$ , under stable and unstable conditions.

Most researchers have described the turbulent exchange processes between land surface and atmosphere as well as ocean and atmosphere in the ABL by using mean profile techniques. Flux-gradient relationships are essential for the synthesizing of turbulent fluxes of momentum and heat, and the predicting of diffusion of pollutants. Unfortunately, there are different forms and constants suggested for the functional representation of non-dimensional gradients, so that it is of interest to find the suitable and the reasonable technique and formulae through some comparison.

In the present paper, we focus on the determining of dimensionless functions of momentum and heat flux under a wide range of stratification conditions in the framework of local similarity theory in terms of three techniques, which adopt direct covariance (eddy correlation), mean wind and temperature profiles and inertia-subrange cospectra techniques, by use of tower-layer data over Beijing City. These methods are used to derive some universal expressions for the dissipation rates, wind shear and heat flux with  $\zeta_1$ , variation of ratio of eddy coefficients as well as the spectral characteristics of turbulence. The results are compared with each other and then checked with well-defined results in the literature.

The mean wind and temperature profiles normalized with local velocity scale  $u_{*1}$  and temperature scale  $T_{*1}$ , respectively, should be the functions of either  $z/L_1$  or  $z/L'_1$

$$\frac{kz}{u_{*1}} \frac{\partial \bar{U}}{\partial z} = \Phi_m, \quad (1)$$

$$\frac{kz}{T_{*1}} \frac{\partial \bar{T}}{\partial z} = \Phi_h, \quad (2)$$

where overbar is a time average, in this paper, the hourly average is taken, and the subscript  $T$  denotes local values, the other relevant local parameters and formulations are listed below as those used by Nieuwstadt (1984) and Xu et al. (1997)

$\bar{U}$	mean horizontal wind speed,
$\bar{T}$	mean temperature,
$L_1$	Monin-Obukhov length = $-\frac{\bar{T}u_*^3}{kgw'\bar{T}'}$ ,
$L'_1$	the length defined by $\frac{u_*}{gk} \frac{\partial \bar{U}}{\partial z} = \frac{\bar{T}}{T_{*1}} \frac{\partial \bar{T}}{\partial z}$ ,
$u, v, w, T$	the fluctuation values of velocity and temperature,
$k$	Von Karman constant = 0.4,
$g$	acceleration due to gravity.

## 2. Techniques

Non-dimensional wind and temperature gradients,  $\Phi_m$  and  $\Phi_h$ , may be computed by either so-called "direct" or "indirect" method. The former involves two techniques, while the latter has one, all of them will be explained, respectively below.

### 2.1 Eddy-correlation technique

$\Phi_m$  and  $\Phi_h$  can be obtained by solving (1) and (2) in terms of local scales of velocity and temperature, and gradients of wind speed and temperature, respectively. The outputs of sonic anemometer can be applied to the calculation of local scales of velocity and temperature by

$$u_{*1}^2 = -\overline{u'w'} \quad (3)$$

$$T_{*1} = -\frac{\overline{w'T'}}{u_{*1}} \quad (4)$$

The wind and temperature gradients,  $\partial\overline{U}/\partial z$  and  $\partial\overline{T}/\partial z$ , can be directly computed by using a differential approximation for the tower level data.

### 2.2 Mean profile technique

It is based on measurements of mean profiles of wind speed  $\overline{U}$  and temperature  $\overline{T}$  in the tower-layer atmosphere. As the above techniques, the non-dimensional gradients of  $\Phi_m$  and  $\Phi_h$  can also be described by (1) and (2) respectively. The mean wind and temperature gradients were estimated as the basic set of computations  $\Phi_m$  and  $\Phi_h$ . According to local similarity (e.g. Al-Jiboori et al., 1999 and Sugita et al., 1995), the fluxes  $u_{*1}$  and  $T_{*1}$  between successive two levels can be calculated by the following expressions:

$$u_{*1} = k(\overline{U}_{i+1} - \overline{U}_i) / [\ln(\frac{z_{i+1}}{z_i}) - \Delta\Psi_m] \quad (5)$$

$$T_{*1} = k(\overline{T}_{i+1} - \overline{T}_i) / [\ln(\frac{z_{i+1}}{z_i}) - \Delta\Psi_h] \quad (6)$$

where

$$\Delta\Psi_m = \int_{z_i}^{z_{i+1}} \frac{1 - \Phi_m}{\zeta'} \quad \text{and} \quad \Delta\Psi_h = \int_{z_i}^{z_{i+1}} \frac{1 - \Phi_h}{\zeta'} \quad (7)$$

are variations of stability correction functions for momentum and heat, respectively, where  $\zeta'$  is  $z/L'_1$ . In this method, the functions  $\Phi_m$  and  $\Phi_h$  are taken as functions of  $z/L'_1$ . The quantity  $L'_1$  is related to  $L_1$  by

$$L_1 = \frac{K_m}{K_h} L'_1 = \frac{L'_1}{\alpha} \quad (8)$$

where  $K_m$  and  $K_h$  are turbulent transfer coefficients for momentum and heat, respectively,  $\alpha$  is defined by

$$\alpha = \frac{K_h}{K_m} = \frac{\overline{w'T'} \partial\overline{U}/\partial z}{\overline{u'w'} \partial\overline{T}/\partial z} \quad (9)$$

In order to solve (5) and (6), we assumed initial values of functions  $\Delta\Psi_m$  and  $\Delta\Psi_h$ , then the iteration method was used to minimize the percentage error.

### 2.3 Inertia-subrange cospectra (ISC) method

The indirect method, which is proposed by Wyngaard and Cote (1972), is based on the relationships of cospectra  $C_{uw}(n)$  and  $C_{wT}(n)$  to vertical gradient  $\partial\overline{U}/\partial z$  and  $\partial\overline{T}/\partial z$  given by the following expressions:

$$nC_{uv}(n) = - \left( \frac{z}{2\pi} \right)^{4/3} \beta \frac{\partial \bar{U}}{\partial z} \varepsilon^{1/3} f^{-4/3}, \quad (10)$$

$$nC_{vT}(n) = - \left( \frac{z}{2\pi} \right)^{4/3} \gamma \frac{\partial \bar{T}}{\partial z} \varepsilon^{1/3} f^{-4/3}, \quad (11)$$

where  $f (= 2\pi n / \bar{U})$  is dimensionless frequency,  $\varepsilon$  is a dissipation rate for TKE,  $\beta$  and  $\gamma$  are non-dimensional cospectral constants. Equations (10) and (11) can be solved by using (1) and (2) as well as the non-dimensional dissipation rate defined as follows:

$$\Phi_\varepsilon = \frac{kz\varepsilon}{u_{*1}^3}, \quad (12)$$

Substituting (1) and (2) into Equations (10) and (11) leads to the following equations:

$$\frac{nC_{uv}(n)}{u_{*1}^2} = - (2\pi k)^{-4/3} \beta \Phi_m \Phi_\varepsilon^{1/3} f^{-4/3}, \quad (13)$$

$$\frac{nC_{vT}(n)}{u_{*1} T_{*1}} = - (2\pi k)^{-4/3} \gamma \Phi_h \Phi_\varepsilon^{1/3} f^{-4/3}. \quad (14)$$

In fact, there are no detailed studies about the estimation of the constants  $\zeta$  and  $\gamma$  except Wyngaard and Cote's paper (1972) (see Fig. 2). Although the combinations  $\beta \Phi_m \Phi_\varepsilon^{1/3}$  and  $\gamma \Phi_h \Phi_\varepsilon^{1/3}$  have been determined by some researchers directly from measurements of cospectra in the inertia-subrange (e.g. Kaimal et al., 1972; Roth and Oke, 1993).

We can get  $\Phi_m$  and  $\Phi_h$  by use of (13) and (14) and the cospectral constants given by Wyngaard and Cote (1972), where  $\Phi_\varepsilon$  was calculated by the following way. The dissipation rate  $\varepsilon$  of TKE was firstly obtained from a regression of the spectral density of the longitudinal velocity in the inertia-subrange of slope  $-5/3$  power law

$$S_{vv}(n) = \alpha_\nu \varepsilon^{2/3} (2\pi n / \bar{U})^{-5/3}, \quad (15)$$

where  $\alpha_\nu$  is the Kolmogorov constant, taken as 0.55 (e.g. Antonia et al., 1979; Kaimal and Finnigan, 1994). Then, by replacing the natural frequency  $n$  with the non-dimensional frequency  $f$  and substituting (12) into (15), Equation (15) becomes

$$\frac{nS_{vv}(n)}{u_{*1}^2} = \alpha_\nu (2\pi k)^{-2/3} \Phi_\varepsilon^{2/3} f^{-2/3}, \quad (16)$$

finally,  $\Phi_\varepsilon$  was estimated by (16).

### 3. Site and data acquisition

The data came from a meteorological tower of 325 m height, located at straight north of Beijing City, 1 km away from Sanhuan Road. In the last two years many high buildings have been set up to the south of this Road 100 m away. The observation field around the tower is a relatively flat field, for planting wheat and short grass. There are several scattered observation rooms not higher than 4 m around the tower. The surface roughness lengths,  $z_0$ , were estimated by Yin and Hong (1999) by using the tower data, according to the wind directions (in degrees). The values of  $z_0$  were 4.0 m for 0–90, 4.5 m for 90–180 and 3.1 m for 270–360.

respectively.

The synchro-measurement for atmospheric pollutants ( $O_3$ ,  $NO_x$ ,  $CO$ ) and meteorological elements (wind, temperature, humidity) in the tower layer was conducted during the period of October 7 to November 6, 1998. Two kinds of meteorological data sets were collected to do this study. The first data-set includes an hourly mean wind speed and temperature profile measurements at all tower levels of 8, 15, 32, 47, 63, 80, 102, 120, 140, 160, 180, 200, 240, 280, 320 m, for five days, October 19 to 23, 1998, which were sampled at a frequency of 3 times per minute. These data were measured by means of Psychrometers and cup-anemometers at northwest and southwest direction. We choose the data in the direction of the northwest according to the prevailing wind direction at that time.

The second data-set, which represents an instantaneous three-component velocities and temperature with sampling frequency of 10 times per second (10 Hz), sampling length of 1 hour, was measured by three dimensional sonic anemometer-thermometer instruments at 47, 140, 280 m levels, during the period of October 14 to 23, 1998.

The instantaneous values of absolute temperature  $T (= |\bar{T} + T'|)$  were obtained from the sound speed measurements obtained from the 3-D sonic anemometer by using the following formula, neglecting water vapor fluctuations (Feynman et al., 1963; Kaimal and Finnigan, 1994)

$$c^2 = 403|\bar{T} + T'| (1 + 0.32e/p) , \quad (17)$$

where  $c$  is the speed of sound,  $e$  is the water vapor pressure and  $p$  is the atmospheric pressure. The temperature data obtained from (15) have been compared with those from a fine wire thermocouple instruments and have been applied successfully in the other studies (Albertson et al., 1995; Kiely et al., 1996).

Before spectra and cospectra were computed by using "Fast Fourier Transform (FFT)" the data preprocessing was made, which included that the coordinate system was transferred into mean wind as the  $X$ -axis direction, a second order polynomial fit was applied for linear detrending and bell tapering was used at 10% of the beginning and ending of the recording length (Stull, 1988). The aliasing was minimized by low-pass filter with an appropriate cut-off frequency at high wavenumbers.

## 4. Results and discussion

### 4.1 Dimensionless wind and temperature gradients

#### 4.1.1 Result for unstable conditions

The non-dimensional gradients of wind and temperature,  $\Phi_m$  and  $\Phi_h$ , evaluated by the three methods mentioned in Section 2, were presented in a wide range of stability parameter  $\zeta_1$  ( $|\zeta_1|$  up to 10). In order to examine the validity of these results as well as the difference between them and the results reported by Hu and Zhang (1993) and Xu et al. (1997), we plot them against stability parameter together in Figs. 1a and 1b for  $\Phi_m$  and  $\Phi_h$ , respectively. The remarks (\*), (+) and (•) are the individual measurement points for  $\Phi_m$  and  $\Phi_h$  calculated by eddy correlation, mean profile and inertia-subrange cospectra methods, respectively. The results from the various methods have similar trend over the entire stability range, but the points derived by the first method are more scatter than those from the other methods. This scatter is due to the direct calculation of  $u_{*1}$  by using (3), which yielded also high scatter for measurements of momentum flux calculated by Al-Jiboori et al. (1999) for the same used data.

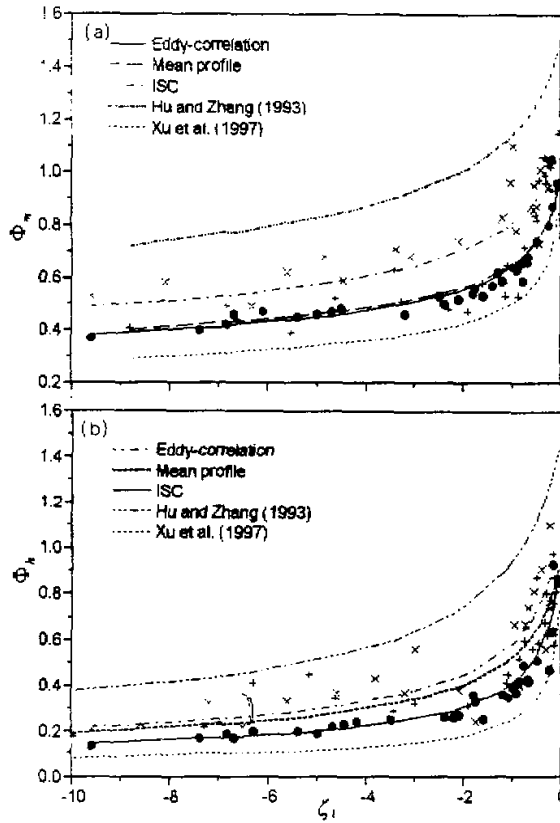


Fig. 1. Non-dimensional gradients of mean wind speed and temperature,  $\Phi_m$  and  $\Phi_h$ , as a function of  $\zeta_1$  under unstable conditions. The symbols  $\times$ ,  $+$  and  $\circ$  denote results of eddy-correlation, mean profiles and ISC methods, respectively.

In this study we use the general expressions of  $\Phi_m$  and  $\Phi_h$ , respectively

$$\Phi_m = a(1 - b\zeta_1)^{-1.4} \quad \zeta_1 < 0 \quad (18)$$

$$\Phi_h = a(1 - b\zeta_1)^{-1.2} \quad \zeta_1 < 0 \quad (19)$$

Each equation contains the empirical constants  $a$  and  $b$ , which are based on observations but the values of  $\Phi_m$  and  $\Phi_h$  are different slightly for observations, with  $a = 1.1, 0.97$  and  $1.0$ , and  $b = 2.5, 3.8$  for  $\Phi_m$  and  $2.4$  for  $\Phi_h$ , and  $4.8$  derived from eddy correlation, mean profiles and ISC methods, respectively, while they were  $1.5$ , and  $2.0$  for  $\Phi_m$  and  $1.5$  for  $\Phi_h$  obtained by Hu and Zhang (1993). Comparing results of the three methods each other and with those reported by Hu and Zhang (1993) and Xu et al. (1997), we can see that all of curves have similar trend near the neutral region, and have apparent separation with the increase of instability, because  $\Phi_m$  and  $\Phi_h$  are sensitive to the magnitudes of  $a$  and  $b$  when  $-\zeta_1$  increases. In addition, the curves from last two methods are often close to each other and to results of Xu et al.

(1997) and Carl et al. (1973), but there is a significant difference between them and those from the eddy correlation method, especially for the results of  $\Phi_m$ .

#### 4.1.2 Results for stable conditions

Most studies of mean wind speed and temperature profiles have found that  $\Phi_m$  and  $\Phi_h$  were proportional to  $\zeta_1$  in the form

$$\Phi_m = \Phi_h = a(1 + b\zeta_1), \quad \zeta_1 > 0 \quad (20)$$

The constants  $a$  and  $b$  were found to be 1.5 and 0.3 by Hu and Zhang (1993) obtained from meteorological tower. Through the fitting of function  $\Phi_m (= \Phi_h)$  calculated by the three methods we found that  $a$  was 0.8, 0.95 and 0.9, and  $b$  was 1.8, 2.7 and 3.6 respectively, which are larger than those given by Hu and Zhang (1993). The values of  $a$  and  $b$  from mean profile and inertia-subrange cospectra methods are very close to results reported by Xu et al. (1997), because the fluctuation data are also from tower-layer atmosphere. We put all of  $\Phi_m$  and  $\Phi_h$  values derived by various methods with the results obtained by Xu et al. (1997) and Hu et al. (1993) into Fig. 2 for comparison.

Figure 2 shows that generally, the scatter of the individual data points for  $\Phi_m$  and  $\Phi_h$  under the stable stratifications is much larger than those under the unstable conditions. Because of the larger scatter for a few data points derived by eddy-correlation, the curve fitted seems relatively away from the curves of other methods. In addition, the curve from the eddy correlation method by Xu et al. (1997) is located between the curves of mean profile and cospectra methods, which confirms the validity of results derived by these two methods. Thus, the results of eddy-correlation may be attributed to the direct use of raw data, in contrast the inertia-cospectra method requires some modifications for these data, which was mentioned in Section 3.

#### 4.2 Average dissipation rate

In fact, the computation of gradient functions of  $\Phi_m$  and  $\Phi_h$  by the ISC method is also the first calculation of the dissipation rates of TKE,  $\Phi_\epsilon$ . This  $\Phi_\epsilon$  is important, which is related

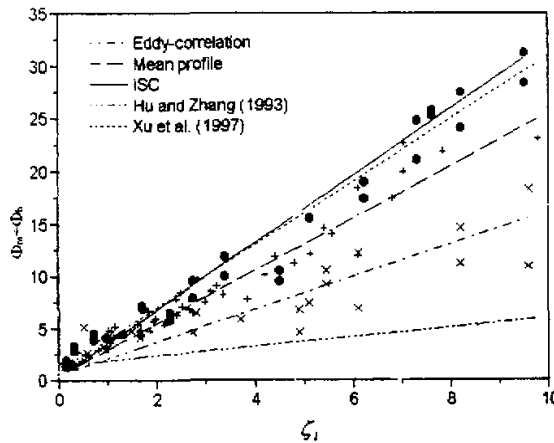


Fig. 2. Same as Fig. 1, but for stable conditions.

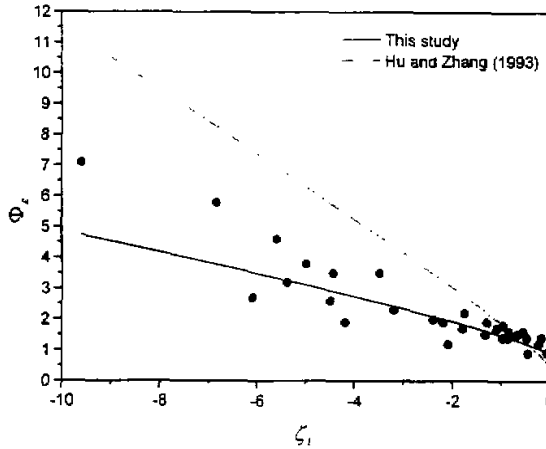


Fig. 3. Non-dimensional dissipation rates for turbulent kinetic energy as a function of  $\zeta_1$  under unstable conditions.

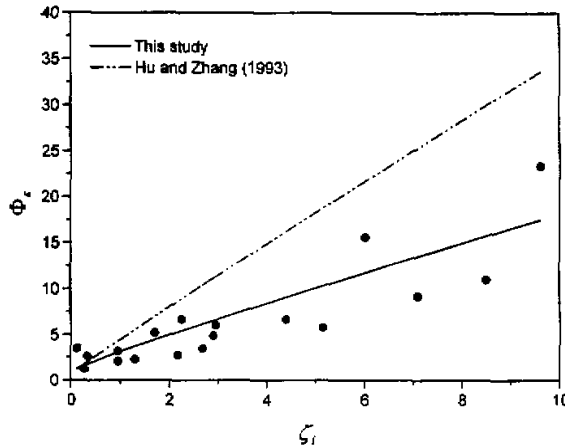


Fig. 4. Same as Fig. 3, but for stable conditions.

to the production rate of TKE through the simplified turbulent kinetic energy budget equation. In this study, however, the normalized dissipation rates,  $\Phi_e$ , were computed directly by using the spectral densities of longitudinal velocity under unstable and stable stratifications as the average over a wide range of band-frequency within the region of '-2/3' slope in the inertia-subrange. Non-dimensional dissipation rates  $\Phi_e$  of power spectra are plotted versus  $\zeta_1$  in Figs. 3 and 4 under unstable and stable conditions with early some results of Hu and Zhang (1993) as a reference paper. The general expression can be used to fit dissipation rates data

$$\Phi_e = a(1 + b|\zeta_1|^{2/3})^{3/2} \quad (21)$$



taking  $\Phi_h$  to be unity at neutral, where  $a$  and  $b$  are the empirical constants. In unstable conditions, initially they were found to be smaller than 0.4 and 1.8 reported by Hu and Zhang (1993). The values of 0.8 and 0.5 were obtained by us in this study represented by the solid line.

For the stable conditions, the values of  $a$  and  $b$  in our study were 0.8 and 1.5, which are also a little smaller than 0.4 and 4.0 suggested by Hu and Zhang (1993). In order to illustrate these differences, the curves fitted were presented in Figs. 3 and 4 under unstable and stable conditions, respectively. We can see that all of these curves go through 1.0 at the origin, but there are apparent differences with the increase of (in-) stability.

#### 4.3 Ratio of eddy diffusivities

In application of the mean wind and temperature profiles technique, we calculated the ratio of eddy thermal diffusivity  $K_h$  to eddy viscosity  $K_m$ , space  $\alpha = K_h / K_m$  under stable and unstable conditions. According to (1), (2), (3), (4) and (12),  $\alpha$  can be represented as

$$\alpha = \frac{\Phi_m}{\Phi_h} \quad (22)$$

Then, we transformed stability parameter  $\zeta'_1$  to  $\zeta_1$  by using (8). This transformation is important to compare results with other methods. There exists considerable uncertainty in variation of  $\alpha$  with  $\zeta_1$  under unstable and stable conditions in the ABL. The values of  $\alpha$  obtained from (22) are shown in Fig. 5 in a wide range of  $|\zeta_1|$ . As the previous discussion in Section 4.1, the scatter of  $\alpha$  on both sides is more than that in  $\Phi_m$  and  $\Phi_h$  plots because  $u_*^2$  is involved (9). Figure 5 shows that the values of  $\alpha$  clearly increase with increasing instability. By substituting (18) and (19) into (23) the following equation represented by the solid line in Fig. 5 is given:

$$\alpha = 1.05(1 - 1.5\zeta_1)^{-1/4} \quad \zeta_1 < 0 \quad (23)$$

It shows clearly that the constant  $\alpha$  is 1.05 at  $\zeta_1 = 0$ , which is very close to 1.0 assumed in

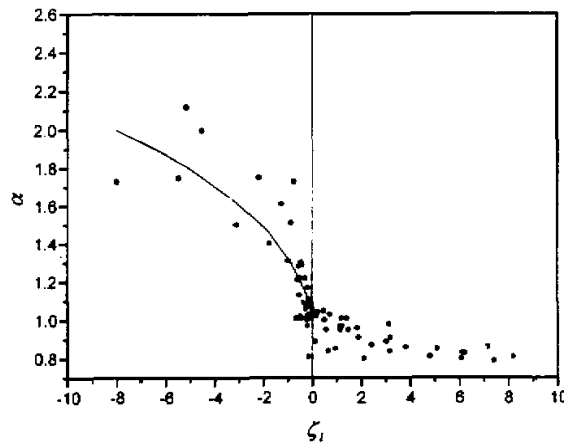


Fig. 5. Ratio of eddy diffusivities,  $\alpha (= K_h / K_m)$  as a function of  $\zeta_1$  for unstable and stable conditions.

Webb (1970), and less than the value of 1.35 suggested by Businger et al. (1971).

In stable air,  $\alpha$  decreases slowly with increasing of  $\zeta_1$  (up to 2.0). This behavior is in good agreement with the result obtained by Businger et al. (1971), but it is incompatible with Carl et al. (1973) and Webb (1970). The average value of  $\alpha$  goes below unity which is about 0.83 if  $\zeta_1 > 2.0$ .

4.4 Normalized spectra and cospectra

If we now divide the left-hand sides of Eqs. (13), (14) and (16) by the quantities  $\Phi_m \Phi_w^{1/3}, \Phi_h \Phi_w^{1/3}$  and  $\Phi_t^{2/3}$  respectively, we remove the stability dependence in their equations. This brings all cospectra / spectra into coincidence in the inertia-subrange, while the cospectra / spectra peaks will spread out at low-frequency parts according to stability. This form of normalization has been applied to the cospectra / spectra presented in Figs. 6 and 7. These figures display spectral behavior of  $u$ , space  $uw$  and  $wT$  versus non-dimensional frequency  $f$  on the log-log plot. However, in order to simplify the analysis of the spectral / cospectral data of this study, the runs were divided into five groups according to stability parameter  $\zeta_1$ , which ranged from -2.0 to +2.0. The boundaries of each group and their remarks were given in the caption of Fig. 6.

It is clear that the normalized spectra / cospectra reduced to a family of curves, which has been found by Kaimal et al. (1972) and Roth and Oke (1993). In addition, the scatter of cospectral data of  $uw$  and  $wT$  in the area of low frequency is more than that of  $u$ -spectral data. It shows that the actual scatter in Fig. 7 is probably a good measure of any statistical quantity (Pond et al., 1971). We can conclude from our results that using the ISC method in calculating the non-dimensional gradients of  $\Phi_m$  and  $\Phi_h$  is a reasonable guide to ensure the validity of cospectra sensitivity measurements.

Figure 6 shows that the  $u$ -spectra follow the '-2/3' power law in inertia-subrange, according to Kolmogorov law of slope '-5/3'. The spectral data cluster of the low frequency appears approximately similar to those given by Kaimal et al. (1972) and Roth and Oke (1993) with a shift of stable spectra peaks towards low frequencies. While the  $wu$ - and

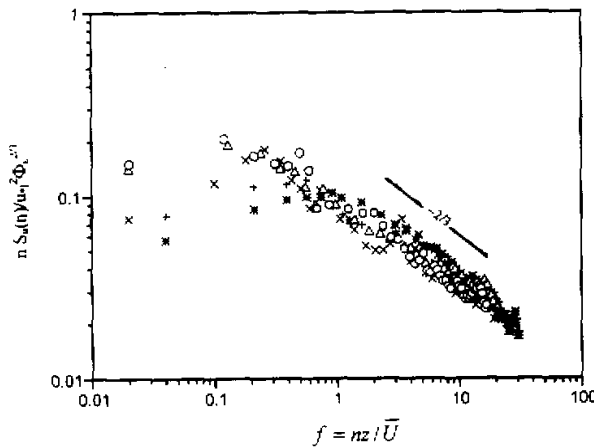


Fig. 6. Normalized  $u$ -spectra for five groups versus non-dimensional frequency  $f$ . Following remarks represent ranges of  $\zeta_1$  value: (\*)  $\rightarrow 0.5 \leq \zeta_1 \leq 2.0$ , space (+)  $\rightarrow 0.11 \leq \zeta_1 \leq 0.27$ , ( $\times$ )  $\rightarrow 0.06 \leq -\zeta_1 \leq 0.2$ , ( $\Delta$ )  $\rightarrow 0.21 \leq -\zeta_1 \leq 0.99$  and (o)  $\rightarrow 1.0 \leq -\zeta_1 \leq 2.0$ .

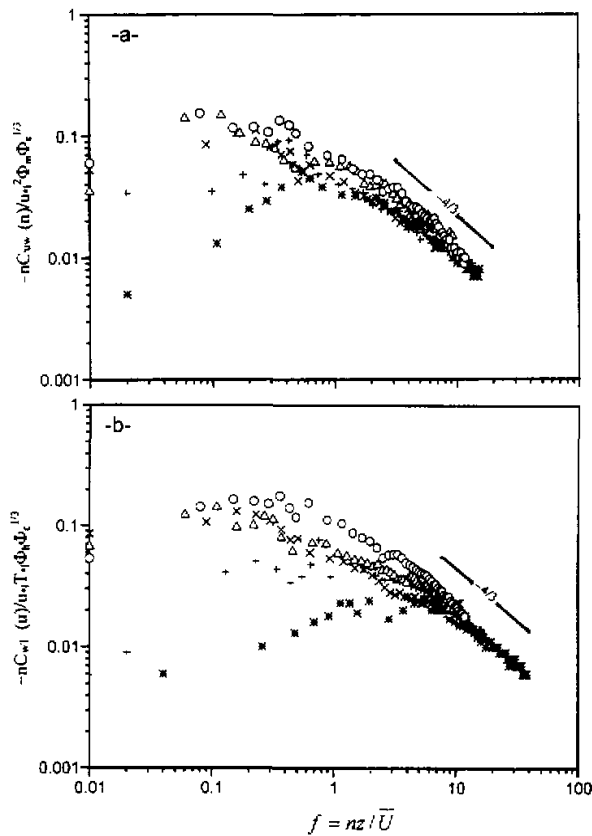


Fig. 7. Same as Fig. 6, but for normalized cospectra (a)  $wv$  and (b)  $wT$ .

$wT$ -cospectra shown in Fig. 7 follow  $\sim 4/3$  power law which decrease more rapidly with frequency than that for spectra. The results from this study are in good agreement with those from Kaimal data, i.e.  $wv$ - and  $wT$ -cospectra crowd into a relatively narrow band at the low-frequency end under unstable conditions, while the location of cospectral peaks shifts as a function of  $\zeta_j$  in stable air.

### 5. Concluding remarks

In this study, local similarity scaling was successfully applied to deriving a number of similarity functions of the single parameter  $z/L_1$  for flux-gradients, dissipation rate and ratio of eddy diffusivities. The non-dimensional wind and temperature gradients,  $\Phi_m$  and  $\Phi_h$ , were calculated by three techniques: eddy-correlation, profiles of mean wind and temperature and ISC method. The empirical constants obtained by (18), (19) and (20) under the unstable and stable conditions are shown as follows:

Condition Method	Unstable		Stable	
	Empirical constants in (18) and (19)		Empirical constants in (20)	
	a	b	a	b
Eddy-correlation	1.1	0.5	0.8	1.8
Mean profile	0.97	3.8 for (18) 2.4 for (19)	0.95	2.7
ISC	1.0	4.8	0.9	3.6

Because the large scatter of the data points calculated by eddy-correlation as well as its values of  $a$  and  $b$  differs from last two techniques and others, we found in our study that the results from the mean profiles and ISC approaches are usually close to each other and similar to that from Xu et al. (1997).

The ISC method being of particular features not only shows that its good results with common results, but also provides an extensive insight of study characteristics of ABL. Besides the computation of  $\Phi_m$  and  $\Phi_w$ , the dissipation rate for turbulence was calculated by using  $u$ -spectra for both unstable and stable conditions.

The ratio of the eddy diffusivities for heat and momentum was estimated to transform  $\zeta_1'$  into  $\zeta_1$  in the application of mean profiles methods. The ratio is a little greater than 1.0 at neutrality; it shows a marked increase when  $\zeta_1' \rightarrow -10$ , and a slow decrease when  $\zeta_1' < 2.0$  and then more constancy appears at  $\zeta_1' > 2.0$ .

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