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# Sensitivity of ocean heating rate estimate to time series processing methods

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19 **Abstract**

20 Ocean heat content (OHC) is a key indicator of global warming, and OHC rate can  
21 be used to quantify Earth's energy imbalance (EEI) as ~90% of EEI is stored in the  
22 ocean. However, when estimating global ocean heating rate that is the first derivative  
23 of OHC ( $dOHC/dt$ ), various time series processing methods were used, including  
24 smoothing, differentiation, and annual mean definition, which introduced differences  
25 in the resultant  $dOHC/dt$  estimate. This study utilized nine OHC datasets to analyze the  
26 impact of the above-mentioned approaches on  $dOHC/dt$  estimation and compared with  
27 the EEI observation at the top of atmosphere. The results show that the choice between  
28 the January-December and July-June annual means introduces 14% relative trend  
29 uncertainty into the estimation of the long-term trend of  $dOHC/dt$ . Different time  
30 derivative methods affect the interannual signal phase and amplitude, where the center  
31 difference for  $dOHC/dt$  and Clouds and the Earth's Radiant Energy System (CERES)  
32 strongest EEI consistency. The smoothing process further enhanced the consistency  
33 between  $dOHC/dt$  and CERES. These results indicate that the choice of time series  
34 processing techniques introduces a non-negligible uncertainty in the OHC-based EEI  
35 estimate. Moreover, this study shows that different OHC datasets show larger  
36 differences compared with the methodology choices, suggesting the data uncertainty is  
37 still the primary source of OHC-based EEI estimation errors. This study provides a  
38 methodological basis for improving EEI estimation and also for the evaluation of

39 climate models with observations.

40 **Key words:** EEI; OHC; Differentiation; Smoothing

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42 **Article Highlights:**

43 ● Smoothing greatly improves correlation between OHC-EEI and CERES-EEI,  
44 especially using the Lanczos filter.

45 ● The July-June annual mean definition enhances consistency between OHC-based  
46 EEI and CERES-EEI compared to the calendar-year mean.

47 ● Different choice of OHC datasets lead to larger EEI difference than time-series  
48 processing methods.

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## 50 **1. Introduction**

51 Earth energy imbalance (EEI) is a crucial metric for climate change, representing  
52 the difference between net solar incoming radiation and outgoing longwave radiation  
53 at the top of the atmosphere (TOA) (Meysignac et al., 2019; von Schuckmann et al.,  
54 2016). Under the influence of human activities, particularly greenhouse gas emissions,  
55 the Earth's energy budget at the TOA has become imbalanced (Hansen et al., 2011;  
56 Johnson et al., 2021; Trenberth et al., 2009). When EEI is positive, it indicates that the  
57 Earth system absorbs more energy than it radiates back to space, leading to continuous  
58 heat accumulation and consequent global warming. Approximately 90% of this excess  
59 energy resulting from EEI is absorbed by the ocean, primarily manifested as a sustained  
60 increase in ocean heat content (OHC) (von Schuckmann et al., 2023). Thus, changes in  
61 OHC have become one of the most widely used method for estimating EEI (Meysignac  
62 et al., 2019). Accurate quantification of OHC and EEI is of fundamental importance for  
63 assessing climate change impacts, evaluating the effectiveness of emission reduction  
64 policies, and evaluating climate models (Cheng et al., 2022a; L'Ecuyer et al., 2015;  
65 Meysignac et al., 2019).

66 Current OHC estimates still have considerable uncertainties. Firstly, the OHC  
67 estimation based on in situ observations is affected by irregular coverage of historical  
68 data and instrument bias (Abraham et al., 2013; Cheng et al., 2018; Domingues et al.,  
69 2008; Gouretski et al., 2007; Lyman et al., 2010; Rhein et al., 2013; Trenberth et al.,  
70 2016; von Schuckmann et al., 2014). Geodetic approach provides an indirect approach

71 of calculating OHC from altimetry and GRACE satellite missions (Hakuba et al., 2021;  
72 Meyssignac et al., 2019). Although this method can provide global coverage, its  
73 observation ability in sea ice area is limited, and is restricted by geophysical correction  
74 error and uncertainties from the thermal expansion coefficient (Ablain et al., 2019;  
75 Caron et al., 2018; Hakuba et al., 2021; Kuhlbrodt et al., 2012; Wiese et al., 2016). In  
76 addition, there are notable differences among reanalysis products in the estimation of  
77 OHC (Hakuba et al., 2024; Meyssignac et al., 2019; Palmer et al., 2015; Storto et al.,  
78 2015). Because of the above-mentioned data and technique differences, there are  
79 substantial uncertainty in calculating EEI ( $dOHC/dt$ ) from OHC time series. A recent  
80 community effort (Hakuba et al., 2024) found that EEI uncertainty varied significantly  
81 among different products. The estimated ocean heat uptake (OHU) rate shows a large  
82 range, from  $0.40 \pm 0.12$  to  $0.96 \pm 0.08$   $W m^{-2}$ , over the period from 2005 to 2019.  $W$   
83  $m^{-2}$  Moreover, the spread of the OHU rate is also large, from  $-0.03 \pm 0.13$   $W m^{-2}$   
84  $decade^{-1}$  to  $1.1 \pm 0.6$   $W m^{-2} decade^{-1}$  (Hakuba et al., 2024).

85         Disclosing the source of errors in OHC and improving the understanding of EEI  
86 become a critical research area. Besides the above-mentioned uncertainty sources, one  
87 source of error is not fully investigated yet: the differences in data processing methods,  
88 including the way of calculating differences, the choice between time sampling and  
89 smoothing processing. These differences in processing methods may have a significant  
90 impact on the results of deriving EEI ( $dOHC/dt$ ) from OHC time series, and thus  
91 become an important source of error. Some aspects of the impacts were already

92 revealed in previous studies. For instance, Trenberth et al. (2016) conducted one-sided  
93 difference calculations on the monthly rate of change of multiple OHC products based  
94 on Argo data and found that the standard deviation of monthly dOHC/dt -based EEI  
95 time series without smoothing was 10-13  $\text{W m}^{-2}$ , much higher than the EEI variation  
96 of  $0.64 \text{ W m}^{-2}$  observed by CERES. Applying a 12-month moving average for  
97 smoothing significantly knocked down the noises and bring the dOHC/dt variation  
98 ( $0.91\sim 1.62 \text{ W m}^{-2}$  among different products) closer to CERES variance than using the  
99 original monthly time series. In contrast, Loeb et al. (2021) employed an overlapping  
100 annual center difference method on the OHC data (by calculating differences between  
101 year-long OHC anomalies at half-year intervals) and resulted an EEI trend estimate of  
102  $0.43 \pm 0.40 \text{ W m}^{-2} \text{ decade}^{-1}$  which was statistically indistinguishable from the satellite-  
103 observed trend of  $0.50 \pm 0.47 \text{ W m}^{-2} \text{ decade}^{-1}$ . Similarly, in a comparison of 21 OHC  
104 datasets, Hakuba et al. (2024) found that data processing methods significantly impact  
105 OHU estimates. Their analysis of 13 products revealed that using the cross-year mean  
106 (Jul.–Jun.), as opposed to the calendar year mean, improved the correlation between  
107 dOHC/dt and CERES EEI across most products, with one product showing a maximum  
108 increase of +0.19.

109 To investigate the sensitivity of dOHC/dt estimates to time series processing  
110 methods, this study uses nine OHC datasets to examine the effects of annual mean  
111 definitions, differencing methods, and smoothing techniques on the results.  
112 Furthermore, root-mean-square error (RMSE) and correlation analysis are used to

113 assess how these processing choices influence the consistency between dOHC/dt and  
114 CERES-EEI. Given that differencing can amplify noise in the datasets, the CERES-EEI  
115 data are integrated for comparison with OHC. Additionally, the dominant sources of  
116 uncertainty in current dOHC/dt estimates are examined. This manuscript is organized  
117 as follows: Section 2 describes the datasets used and data processing methods. Section  
118 3 presents the results, illustrating the impacts of smoothing, differencing, annual mean  
119 definition, and monthly processing approaches on dOHC/dt estimation, and attributes  
120 the primary sources of uncertainty. Section 4 contains conclusion and discussion.

## 121 **2. Data and Method**

### 122 *2.1 Data*

123 This study selected nine global OHC datasets (Table 1), covering various  
124 observational sources and processing methods to ensure the comprehensiveness of the  
125 analysis and the reliability of the conclusions. The dataset includes five data sets based  
126 on in situ observations, two reanalysis products, one product based on satellite sea level  
127 height reconstruction, and one product integrating multi-source observations and  
128 models. The in situ observations of OHC are from the following data sets EN4 (Good  
129 et al., 2013), Scripps Institution of Oceanography (SIO) (Roemmich et al., 2009),  
130 Institute of Atmospheric Physics (IAP , version 4.2) (Cheng et al., 2024; Cheng et al.,  
131 2017; Cheng et al., 2016), Japan Agency for Marine-Earth Science and Technology  
132 (JAMSTEC) (Hosoda et al., 2008), Ishii (Ishii et al., 2017). Two reanalysis products

133 include Estimating the Circulation and Climate of the Ocean (ECCO, version 4) (Forget  
134 et al., 2015) and Ocean Reanalysis System 5 (ORAS5) (Zuo et al., 2019). The product  
135 based on satellite sea-level height reconstruction is from the Laboratoire d'Etudes en  
136 Géophysique et Océanographie Spatiales (LEGOS) (Marti et al., 2022). The dataset  
137 integrating multi-source observations and models is sourced from the Pacific Marine  
138 Environmental Laboratory (PMEL) in the United States, specifically from the Random  
139 Forest Regression Ocean Maps (RFROM) analysis system (Lyman et al., 2023). These  
140 datasets vary significantly in terms of spatial resolution, observation methods, and error  
141 structure, providing diverse test conditions for the comparison of different processing  
142 methods. Observations after 2005 and ocean depths 0-2000 m were used in this study,  
143 mainly because the Argo network achieves near-global open ocean coverage, which  
144 significantly improves the quality and consistency of OHC and makes EEI analysis  
145 more reliable.

146 The net TOA radiation fluxes are obtained from the Clouds and the Earth's Radiant  
147 Energy System Energy Balanced and Filled (CERES-EBAF) dataset, version 4.2 (Loeb  
148 et al., 2018). The CERES instrument suite is composed of wide-band radiometers  
149 carried by multiple satellites, designed to precisely measure the Earth's radiation budget.  
150 Since March 2000, the CERES instrument has been continuously operating on satellite  
151 platforms such as Tropical Rainfall Measuring Mission (TRMM), Terra, Aqua, Suomi  
152 National Polar-orbiting Partnership (S-NPP) and National Oceanic and Atmospheric  
153 Administration 20 (NOAA-20), accumulating over two decades of global shortwave

154 and long-wave radiation data. The EBAF processing ensures consistency between the  
 155 CERES observations and energy balance constraints by applying bias corrections and  
 156 energy balance adjustments, thereby yielding radiation fluxes that are widely regarded  
 157 as the benchmark for Earth's radiation budget studies. The EBAF-TOA-Level 3b  
 158 product employed in this study provides monthly mean incoming solar radiation, TOA  
 159 fluxes (including short-wave, long-wave radiation fluxes and net fluxes), and cloud  
 160 parameter products based on CERES-MODIS inversion at a spatial resolution of  $1^\circ \times 1^\circ$ .  
 161 Through time integration and calibration, the dataset also delivers consistent long-term  
 162 radiation flux time series that are widely used to assess the Earth's radiation budget and  
 163 energy imbalance. In this study, we selected the period from January 2005 to October  
 164 2023 as the analysis period to match the observation cycle of changes in ocean heat  
 165 absorption.

166 **Table 1.** Description of the datasets used in this study.

<b>Product name</b>	<b>Time range</b>	<b>Spatial range</b>	<b>Time resolution</b>	<b>Spatial resolution</b>	<b>Interpolation method</b>
<b>objective analysis data</b> IAPv4	1940-Present	Global	Monthly	$1^\circ \times 1^\circ$	Ensemble Optimal Interpolation with dynamic ensemble
Ishii	1955-2024	Global	Yearly	$1^\circ \times 1^\circ$	3-D Variational Approach
EN4	1900-Present	Global	Monthly	$1^\circ \times 1^\circ$	Optimal Interpolation (using the Analysis Correction scheme)
SIO	2004-Present	Global	Monthly	$1^\circ \times 1^\circ$	Weighted Least-Squares Fit + Objective Analysis
JAMSTEC	2001-2022	Global	Monthly	$1^\circ \times 1^\circ$	Optimal

						interpolation
<b>reanalysis data</b>						
ECCO	1992-2024	Global	Monthly	0.5°×0.5°	4D	Variational Data assimilation approach
ORAS5	1979-present	Global	Monthly	1°×1°	3D	Variational Data assimilation approach
<b>Satellite-based data</b>						
LEGOS	2002-2020	Global	Monthly	3°×3°	Altimetry	sea level, GRACE
CERES	2000-2025	Global	Monthly	1°×1°	TOA radiation	
<b>fused data</b>						
PMEL	1993-2024	Global	Monthly	0.25°×0.25°	Machine learning	(Random Forest Regression)
RFROM						

## 167 **2.2 Method**

168 To investigate the sensitivity of dOHC/dt estimates to time series processing  
169 methods, this study designed and compared several workflows. These workflows  
170 combine established methods from the literature with new approaches introduced for  
171 this analysis. For clarity, all processing strategies are summarized in Table 2. The  
172 individual steps involved, including time series type, smoothing, and differentiation,  
173 are detailed in the subsequent sections.

174 The time series processing methods selected in this study are intended to cover the  
175 most commonly used and representative categories of techniques in the literature. The  
176 forward, central, and backward difference methods are the three fundamental building  
177 blocks of finite differencing. The choice of smoothing methods encompasses a range  
178 from simple n-point moving averages (MA, WMA) to commonly used filters with high  
179 frequency response characteristics, such as the Butterworth and Lanczos filters, all of

180 which are widely applied in classical oceanographic and climate data analysis (e.g.,  
 181 Hakuba et al., 2024; Trenberth et al., 2016). The calendar-year and cross-year annual  
 182 mean definitions are the two most discussed schemes in the current community.  
 183 Therefore, the analytical framework of this study aims to systematically quantify the  
 184 sensitivity of dOHC/dt estimates to these selected and representative processing  
 185 methods.

186 **Table 2.** Summary of time series processing methods for dOHC/dt estimation  
 187 examined in this study.

<b>ID</b>	<b>Time Series Type</b>	<b>Smoothing Method</b>	<b>Differentiation Method</b>	<b>Reference</b>
1	Monthly	13-month moving average (with end weights of 0.5)	Center difference	Smoothing based on (Trenberth et al., 2016)
2	Monthly	25-month moving average (with end weights of 0.5)	Center difference	
3	Annual (Calendar Year /Cross Year)	None (RAW)	Center difference	
4	Annual (Calendar Year /Cross Year)	Moving average (3-year)	Center difference	Smoothing based on (Abraham et al., 2013)
5	Annual (Calendar Year /Cross Year)	Non-equal-weighted moving mean (0.5-1-0.5) (3-year)	Center difference	
6	Annual (Calendar Year /Cross Year)	Lanzcos filter (3-year cutoff)	Center difference	Smoothing based on (Hakuba et al., 2024)
7	Annual (Calendar Year /Cross Year)	Butterworth filter (3-year)	Center difference	(Roberts et al., 2017)

8	Annual (Calendar Year /Cross Year)	None (RAW)	Forward difference	
9	Annual (Calendar Year /Cross Year)	Moving average (3- year)	Forward difference	Smoothing based on (Abraham et al., 2013)
10	Annual (Calendar Year /Cross Year)	Non-equal-weighted moving mean (0.5-1- 0.5) (3-year)	Forward difference	
11	Annual (Calendar Year /Cross Year)	Lanczos filter (3-year cutoff)	Forward difference	Smoothing based on (Hakuba et al., 2024)
12	Annual (Calendar Year /Cross Year)	Butterworth filter (3- year)	Forward difference	Smoothing based on (Roberts et al., 2017)
13	Annual (Calendar Year /Cross Year)	None (RAW)	Backward difference	
14	Annual (Calendar Year /Cross Year)	Moving average (3- year)	Backward difference	Smoothing based on (Abraham et al., 2013)
15	Annual (Calendar Year /Cross Year)	Non-equal-weighted moving mean (0.5-1- 0.5) (3-year)	Backward difference	
16	Annual (Calendar Year /Cross Year)	Lanczos filter (3-year cutoff)	Backward difference	Smoothing based on (Hakuba et al., 2024)
17	Annual (Calendar Year /Cross Year)	Butterworth filter (3- year)	Backward difference	Smoothing based on (Roberts et al., 2017)

188 *2.2.1 Smoothing*

189 This study tested multiple smoothing methods to evaluate the impact of  
190 suppressing high-frequency noise on dOHC/dt estimation. For annual-mean time series,  
191 four methods were compared: the Lanczos low-pass filter (3-year cutoff period)

192 (Hakuba et al., 2024), a 3-point weighted moving average (WMA, weights 0.5-1-0.5),  
 193 a 3-year simple moving average (MA) (Abraham et al., 2013), and the Butterworth low-  
 194 pass filter (3-year cutoff period) (Roberts et al., 2017). Furthermore, for comparison  
 195 with the annual processing workflow, two smoothing methods applied directly to  
 196 monthly time series were introduced, both following the approach of (Trenberth et al.,  
 197 2016): one is their proposed 13-month running mean (with end weights of 0.5), and the  
 198 other is an extended 25-month running mean (with end weights of 0.5) designed to  
 199 further suppress interannual variability.

### 200 2.2.2 Differentiation

201 Three differential methods are used to calculate the time derivative of OHC  
 202 (dOHC/dt):

$$203 \quad \left. \frac{dOHC}{dt} \right|_{t=t_i} = \begin{cases} \frac{OHC(t_i + \Delta t) - OHC(t_i)}{\Delta t}, & \text{Forward difference} \\ \frac{OHC(t_i + \Delta t) - OHC(t_i - \Delta t)}{2\Delta t}, & \text{Center difference} \\ \frac{OHC(t_i) - OHC(t_i - \Delta t)}{\Delta t}, & \text{Backward difference} \end{cases}$$

204 Where  $OHC(t_i)$  is the OHC at time  $t_i$ ,  $\left. \frac{dOHC}{dt} \right|_{t=t_i}$  is the rate of change of OHC at  
 205 time  $t_i$ , and  $\Delta t$  is the time interval between two adjacent records.

206 In this study, the above three difference methods were applied to the processed  
 207 OHC time series to calculate dOHC/dt. The time step ( $\Delta t$ ) is determined by the  
 208 inherent time resolution of the final smoothed sequence. Therefore, for the annual time  
 209 series,  $\Delta t$  is one year; For the monthly time series,  $\Delta t$  is one month. The OHU time

210 series data is derived from the time derivative calculation of OHC and is ultimately  
211 normalized through the area of the top of the atmosphere (TOA) at a height of 20  
212 kilometers on the Earth's surface, which is  $5.14 \times 10^{14}$  square meters.

### 213 2.2.3 Annual mean definition

214 This study used two definitions to define annual mean: January-December mean  
215 and July-June mean. The later consider the influence of El Niño-Southern Oscillation  
216 (ENSO), which always peaks at winter (Rasmusson et al., 1982).

### 217 2.2.4 Comparison with CERES

218 Because doing the time derivative will certainly amplify the noise in data, this study  
219 also performed an additional comparison between OHC and EEI: doing the time  
220 integration of CERES net radiation flux data to obtain the cumulative energy series,  
221 and remove the linear trend and then compare the result with de-trended OHC time  
222 series for their inter-annual to decadal scale changes. To derive the ocean warming  
223 acceleration, we performed quadratic polynomial fitting on OHC.

224 To quantify the differences between the processed dOHC/dt sequence and the  
225 CERES EEI sequence, this study adopts the Pearson correlation coefficient (R) and root  
226 mean square error (RMSE) as two key metrics:

$$227 \quad R = \frac{\sum_{i=1}^n (r_i - \bar{r})(s_i - \bar{s})}{\sqrt{\sum_{i=1}^n (r_i - \bar{r})^2 \sum_{i=1}^n (s_i - \bar{s})^2}}$$
$$228 \quad RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (r_i - s_i)^2}$$

229 Where  $r_i$  represents the warming rate (OHU) at different time points calculated

230 by various methods,  $s_i$  denotes the processed CERES radiative values at  
231 corresponding time steps,  $\bar{r}$  is the mean of  $r_i$  and  $\bar{s}$  is the mean of  $s_i$ .

232 Within the framework of this study, these two indicators were employed to assess  
233 different aspects of consistency. The RMSE mainly quantifies the average magnitude  
234 of the absolute error between two time series at each time point. While the Pearson  
235 correlation coefficient ( $r$ ) mainly measures the similarity in the form and phase  
236 consistency of the interannual fluctuations of the two sequences. By combining the use  
237 of these two indicators, the consistency of the estimated dOHC/dt results in terms of  
238 numerical deviation and temporal evolution pattern with CERES can be simultaneously  
239 evaluated.

### 240 **3. Results**

#### 241 ***3.1 Smoothing Method Sensitivity***

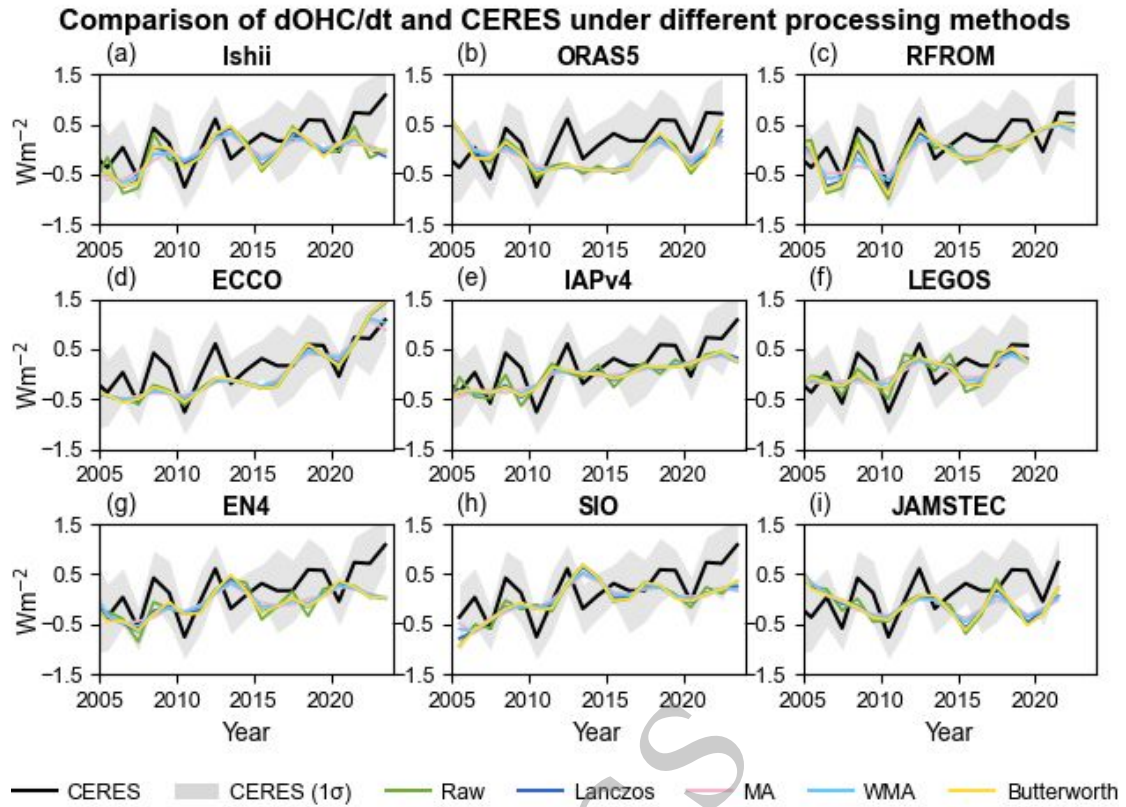
242 The choice of smoothing method affects the estimation of dOHC/dt, including its  
243 interannual variability and long-term trend. Figure 1a compares the dOHC/dt anomaly  
244 series after applying different smoothing methods to various datasets. Taking the Ishii  
245 dataset as an example (Figure 1a), the values of the dOHC/dt anomaly series processed  
246 by different smoothing methods can differ by up to  $0.53 \text{ W m}^{-2}$  in peak years such as  
247 2008. The smoothing differences results in an estimated linear trend for 2005–2024  
248 ranging from  $0.27$  to  $0.29 \text{ W m}^{-2} \text{ decade}^{-1}$ . Further analysis across all datasets shows  
249 that applying a series of smoothing treatments reduces the interannual standard  
250 deviation of dOHC/dt by an average of  $0.07 \text{ W m}^{-2}$  (Table 3) compared to the  
251 unsmoothed RAW series, indicating the suppressive effect smoothing on interannual

252 variability.

253 At the same time, the choice of smoothing method (including RAW series) alone  
254 introduces an average uncertainty (measured by standard deviation) in the estimated  
255 long-term trend of  $0.02 \text{ W m}^{-2} \text{ decade}^{-1}$  (Table 4). Relative to the overall mean trend  
256 ( $0.33 \text{ W m}^{-2} \text{ decade}^{-1}$ ) across all datasets and smoothing methods, this difference  
257 constitutes approximately 6% relative uncertainty, which is important for accurately  
258 assessing the Earth's energy budget. Among all datasets, the trend estimation for ECCO  
259 shows the highest sensitivity (standard deviation = 0.05) to the choice of smoothing  
260 method, while ORAS5 shows the lowest sensitivity. These results indicate that the  
261 choice of smoothing method is a source of uncertainty that should be quantified in the  
262 estimation of the long-term trend of  $d\text{OHC}/dt$ .

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265 **Figure 1.** Impacts of different smoothing methods on dOHC/dt calculation compared  
 266 with CERES data after central differencing. Each panel represents a OHC dataset.  
 267 Different lines correspond to various smoothing methods and the solid black line  
 268 represents results from CERES data, with the gray shaded area indicating the  $\pm 1$   
 269 standard deviation ( $\pm 1\sigma$ ) range, calculated from the 12 monthly CERES values within  
 270 each year. Unit:  $\text{W m}^{-2}$ .

271

272 **Table 3.** Quantification of the effect of smoothing on the interannual standard  
 273 deviation of dOHC/dt anomalies. Unit:  $\text{W m}^{-2}$ . "Std Dev (RAW)" is the standard  
 274 deviation of the original sequence; "Mean Std Dev (Smoothed)" is the arithmetic mean  
 275 of the standard deviations obtained after each dataset is processed by four smoothing

276 methods respectively. "Reduction" is listed as the difference between the two. The  
 277 interannual standard deviation of CERES-EEI is  $0.48 \text{ W m}^{-2}$ .

<b>Dataset</b>	<b>Std Dev (RAW)</b>	<b>Mean Std Dev (Smoothing)</b>	<b>Reduction</b>
Ishii	0.37	0.29	0.08
ORAS5	0.32	0.26	0.06
RFROM	0.45	0.36	0.09
ECCO	0.57	0.52	0.05
IAPv4	0.29	0.25	0.04
LEGOS	0.32	0.22	0.10
EN4	0.31	0.26	0.05
SIO	0.38	0.33	0.05
JAMSTEC	0.29	0.22	0.07
<b>Average</b>	<b>0.37</b>	<b>0.30</b>	<b>0.07</b>

278

279 **Table 4.** Quantification of uncertainty in  $d\text{OHC}/dt$  trend estimates ( $\text{W m}^{-2} \text{ decade}^{-1}$ )

280 arising from the choice of smoothing method.

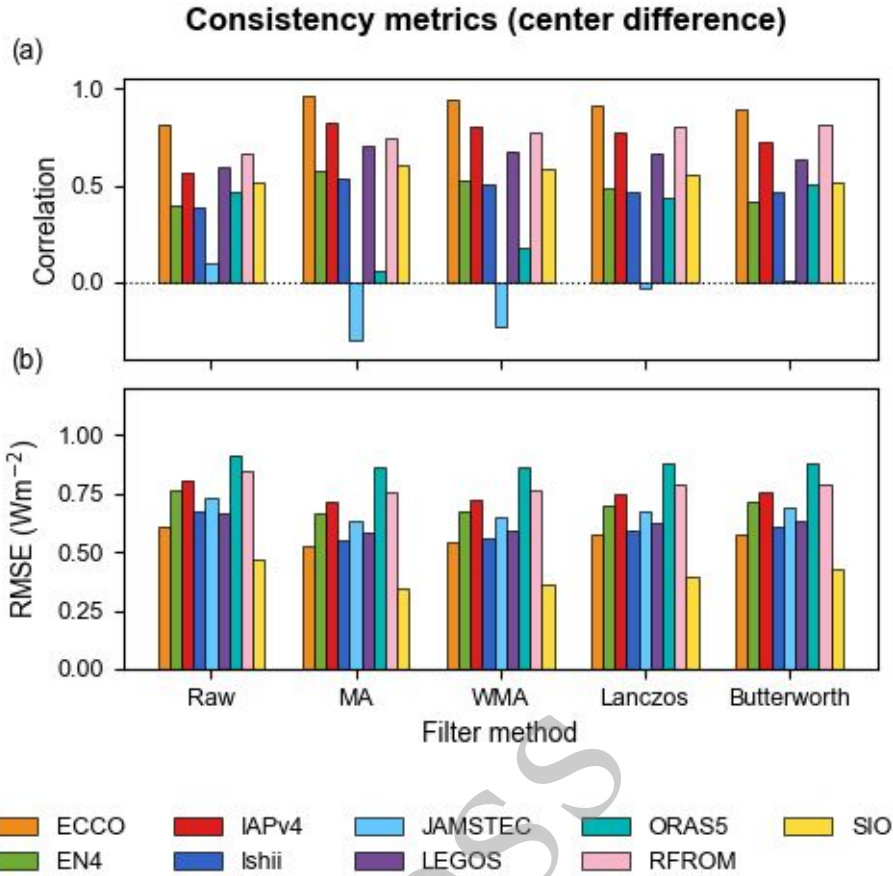
<b>Dataset</b>	<b>Trend MA3</b>	<b>Trend WMA3</b>	<b>Trend Lanzcos</b>	<b>Trend Butterworth</b>	<b>Trend Uncertainty</b>
Ishii	0.27	0.27	0.29	0.29	0.01
ORAS5	0.05	0.05	0.06	0.06	0.01
RFROM	0.50	0.51	0.56	0.53	0.03
ECCO	0.78	0.81	0.89	0.89	0.05
IAPv4	0.38	0.38	0.41	0.40	0.01
LEGOS	0.29	0.30	0.33	0.34	0.02
EN4	0.29	0.29	0.31	0.31	0.01
SIO	0.36	0.38	0.42	0.44	0.04
JAMSTEC	-0.09	-0.09	-0.11	-0.09	0.01
<b>Average</b>	<b>0.30</b>	<b>0.31</b>	<b>0.35</b>	<b>0.36</b>	<b>0.02</b>

281

282       On the other hand, in the comparison between OHC-based EEI and CERES-EEI,  
283 the positive role of smoothing is mainly reflected in the improvement of correlation.  
284 The time series (Figure 1a) shows that the smoothed OHC-based EEI from various  
285 datasets exhibits better agreement with CERES-EEI in certain years than the raw time  
286 series. For instance, in 2008, most OHC datasets under different smoothing methods  
287 show large positive EEI values, corresponding to the high value observed by CERES  
288 in that year. However, noticeable discrepancies remain in some periods. For example,  
289 while CERES observations show a significantly high EEI value in 2015, none of the  
290 OHC datasets reproduce this enhanced signal. To quantitatively evaluate these  
291 observations, Figure 2 presents the RMSE and Pearson correlation coefficient between  
292  $dOHC/dt$  and CERES-EEI.

293

in press



294

295 **Figure 2.** Quantitative comparison of dOHC/dt estimates with CERES-EEI, showing  
 296 the impacts of different smoothing methods and datasets. a) the Pearson correlation  
 297 coefficients and b) the Root Mean Square Error (RMSE) in  $W m^{-2}$ .

298

299 Quantitative analysis of RMSE (Figure 2b) indicates that smoothing had a limited  
 300 impact on reducing the overall error level between OHC-based EEI and CERES-EEI.

301 On average, across the nine datasets, applying smoothing reduced the RMSE by only

302  $0.07 W m^{-2}$  on average compared to the unsmoothed RAW series (Table 5). Unlike the

303 stability of RMSE, the Pearson correlation coefficient showed sensitivity to the choice

304 of smoothing method (Figure 2a). All smoothing methods improved the correlation

305 between OHC-based EEI and CERES-EEI to varying degrees. The results show that

306 compared to the RAW series (mean  $r = 0.55$ ), smoothing increased the mean correlation  
 307 coefficient to above 0.62 (excluding the JAMSTEC outlier). Among the methods, the  
 308 Lanczos filter produced the most notable average improvement, systematically  
 309 increasing the mean correlation coefficient to 0.64. The Lanczos and Butterworth filters  
 310 demonstrated relatively stronger stability in enhancing correlation, maintaining it above  
 311 0.4 for most datasets (except JAMSTEC) and avoiding extreme outcomes like those  
 312 sometimes seen with MA. However, no single method achieved optimal results under  
 313 all circumstances.

314 **Table 5.** Quantification of the effect of smoothing on the RMSE between dOHC/dt  
 315 anomalies and the CERES-EEI reference. Unit:  $\text{W m}^{-2}$ .

Dataset	RMSE(RAW)	Mean RMSE (Smoothing)	RMSE Reduction
Ishii	0.67	0.58	0.09
ORAS5	0.91	0.87	0.04
RFROM	0.85	0.78	0.07
ECCO	0.61	0.55	0.06
IAPv4	0.81	0.73	0.08
LEGOS	0.67	0.61	0.06
EN4	0.76	0.69	0.07
SIO	0.47	0.38	0.09
JAMSTEC	0.74	0.66	0.08
<b>Average</b>	<b>0.72</b>	<b>0.65</b>	<b>0.07</b>

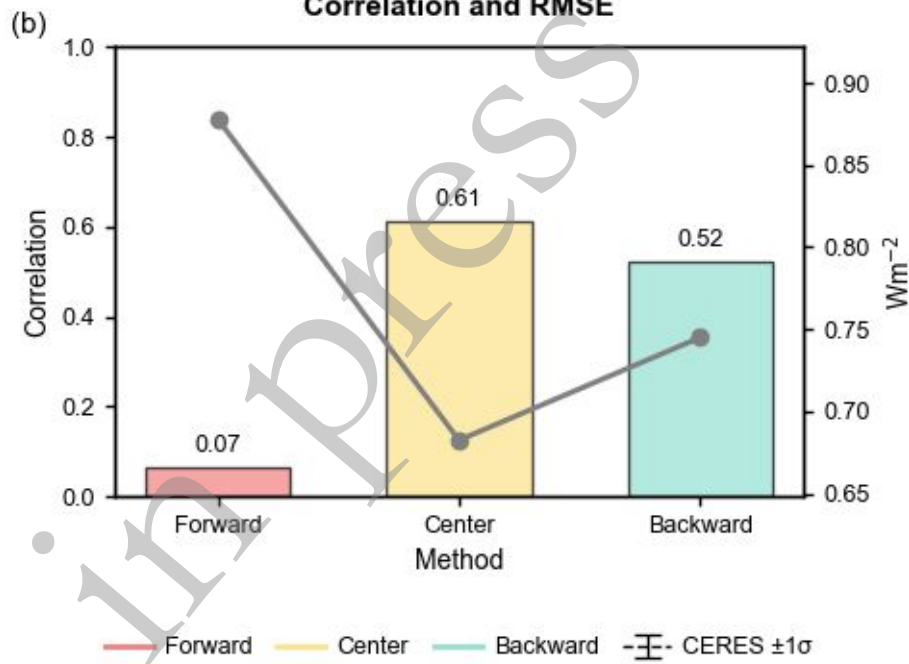
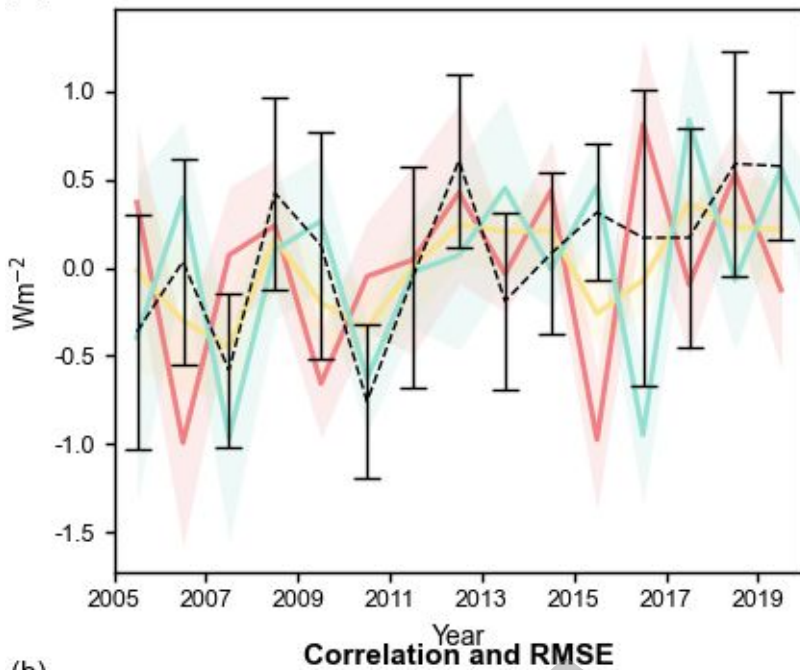
### 316 **3.2 Differentiation Sensitivity**

317 The choice of differencing method introduces uncertainties in both phase and  
 318 amplitude of the interannual signal in dOHC/dt estimates. Figure 3a shows the dOHC/dt

319 results obtained by applying three different differencing methods to the unsmoothed  
320 ensemble mean series (RAW). As illustrated in Figure 3a, the choice of differencing  
321 method leads to phase shifts in the peaks and troughs of the dOHC/dt series. These  
322 phase shifts translate into instantaneous estimation differences during years with strong  
323 interannual variability. For instance, in 2007, the difference between the values  
324 calculated using forward and backward differences reached  $1.4 \text{ W m}^{-2}$ . Furthermore, in  
325 terms of the amplitude of interannual variability, both forward difference (standard  
326 deviation =  $0.40 \text{ W m}^{-2}$ ) and backward difference (standard deviation =  $0.43 \text{ W m}^{-2}$ )  
327 exhibit larger amplitude fluctuations compared to the central difference (standard  
328 deviation =  $0.27 \text{ W m}^{-2}$ ). Additionally, for the estimation of the long-term trend, the  
329 uncertainty in trend introduced by the choice of differencing method (measured by the  
330 standard deviation of the trend values) is  $0.04 \text{ W m}^{-2} \text{ decade}^{-1}$ . This constitutes a  
331 relative uncertainty of approximately 14% relative to the overall mean trend ( $0.29 \text{ W}$   
332  $\text{m}^{-2} \text{ decade}^{-1}$ ) across the different differencing methods.

333

(a) Comparison of dOHC/dt using differentiation methods



334

335 **Figure 3.** Impacts of different differentiation methods on the multi-dataset average

336 dOHC/dt and its consistency with CERES-EEI. a) Compare the time series of the multi-

337 dataset average dOHC/dt calculated using forward, center, and backward difference

338 methods. The shaded areas represent the  $\pm 1$  standard deviation range across the nine

339 OHC datasets for each respective method. The black dashed line with error bars shows  
340 the CERES-EEI benchmark and its intra-annual  $\pm 1\sigma$  range. b) Present the quantitative  
341 comparison with CERES, showing the Pearson correlation coefficient (bars) and the  
342 RMSE in  $\text{W m}^{-2}$  (gray line) for each differentiation method. All calculations are based  
343 on the unsmoothed (Raw) calendar-year (Jan-Dec) annual mean series.

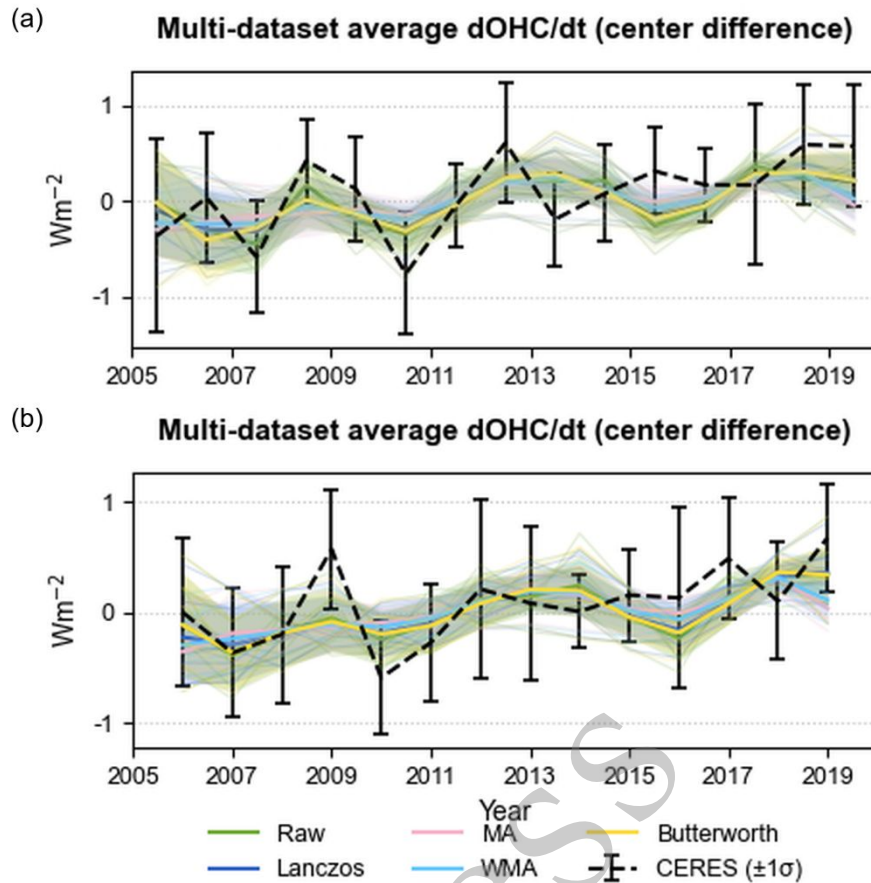
344

345 In the comparison with CERES-EEI, none of the three differencing methods fully  
346 captured the complete interannual signal variations of CERES-EEI in terms of the time  
347 series morphology (Figure 3a). To quantitatively assess this uncertainty, Figure 3b  
348 presents the Pearson correlation coefficients and RMSE between  $d\text{OHC}/dt$  and CERES-  
349 EEI for the three differencing methods. Specifically, the central difference method  
350 achieved a correlation coefficient of 0.61, which is higher than that of the backward  
351 difference (0.52) and the forward difference (0.07). Furthermore, the central difference  
352 also yielded the lowest RMSE ( $0.69 \text{ W m}^{-2}$ ), outperforming the backward difference  
353 ( $0.74 \text{ W m}^{-2}$ ) and the forward difference, which had the largest error ( $0.88 \text{ W m}^{-2}$ ). In  
354 summary, the forward difference introduced the largest error and the lowest correlation;  
355 the backward difference performed moderately; while the central difference  
356 demonstrated the most robust and accurate performance across all evaluation metrics.  
357 Therefore, this study selects the central difference method as the standard  
358 computational approach for all subsequent work.

359

### 360 **3.3 Annual Mean Definition Sensitivity**

361 Figure 4 compares the ensemble mean dOHC/dt series obtained using different  
362 smoothing methods under the calendar year (January–December) and cross-year (July–  
363 June of the following year) averaging definitions. Comparison reveals that the choice  
364 of annual averaging definition alters the phase and shape of the interannual signal in  
365 dOHC/dt. For instance, under the calendar year average (Figure 5a), the mean curve  
366 from all datasets forms a peak during the 2016–2017 period, whereas under the cross-  
367 year average (Figure 5b), this period exhibits a flat trend. Quantifying the amplitude  
368 shows that using the cross-year average reduces the interannual standard deviation of  
369 the ensemble mean (RAW) series from  $0.25 \text{ W m}^{-2}$  (calendar year) to  $0.22 \text{ W m}^{-2}$ . This  
370 suggests that the cross-year averaging definition, by aligning with the natural cycles of  
371 key climate modes such as ENSO, physically better represents the interannual signals.  
372 Furthermore, for the estimation of the long-term trend, the uncertainty in trend  
373 introduced by the choice of annual averaging definition (measured by standard  
374 deviation) is  $0.05 \text{ W m}^{-2} \text{ decade}^{-1}$ . This constitutes a relative uncertainty of  
375 approximately 14% relative to the overall mean trend ( $0.35 \text{ W m}^{-2} \text{ decade}^{-1}$ ).



376

377

378 **Figure 4.** Impacts of different annual mean definitions on the multi-dataset average  
 379 dOHC/dt. a) The multi-dataset average dOHC/dt time series under the calendar-year  
 380 (Jan-Dec) definition. The thick colored lines represent the ensemble average for each  
 381 of the five smoothing methods. The thin, semi-transparent background lines show the  
 382 results from individual OHC datasets, and the shaded area represents their  $\pm 1$  standard  
 383 deviation range. The black dashed line with error bars shows the CERES-EEI  
 384 benchmark and its intra-annual  $\pm 1\sigma$  range. b) Same as in a), but for the cross-year (Jul-  
 385 Jun) annual mean definition.

386

387 In the comparison with CERES-EEI, the time series (Figure 4) shows that during  
388 certain periods (2015–2016), the cross-year average yields better alignment between  
389 the dOHC/dt series and the CERES-EEI curve. A quantitative analysis was conducted  
390 by calculating the RMSE and Pearson correlation coefficient for the unsmoothed RAW  
391 series under different annual averaging definitions. The calculation results show that  
392 adopting the cross-year mean leads to a consistent improvement in both metrics, with  
393 the RMSE decreasing from  $0.68 \text{ W m}^{-2}$  (calendar year) to  $0.67 \text{ W m}^{-2}$ , while the  
394 Pearson correlation coefficient simultaneously increases from 0.61 (calendar year) to  
395 0.63.  $\text{W m}^{-2} \text{ W m}^{-2}$  This indicates that the cross-year average, by avoiding the truncation  
396 of interannual signals in the dOHC/dt calculation to some extent, physically reduces  
397 estimation uncertainty and thereby enhances the consistency between dOHC/dt and  
398 CERES-EEI.

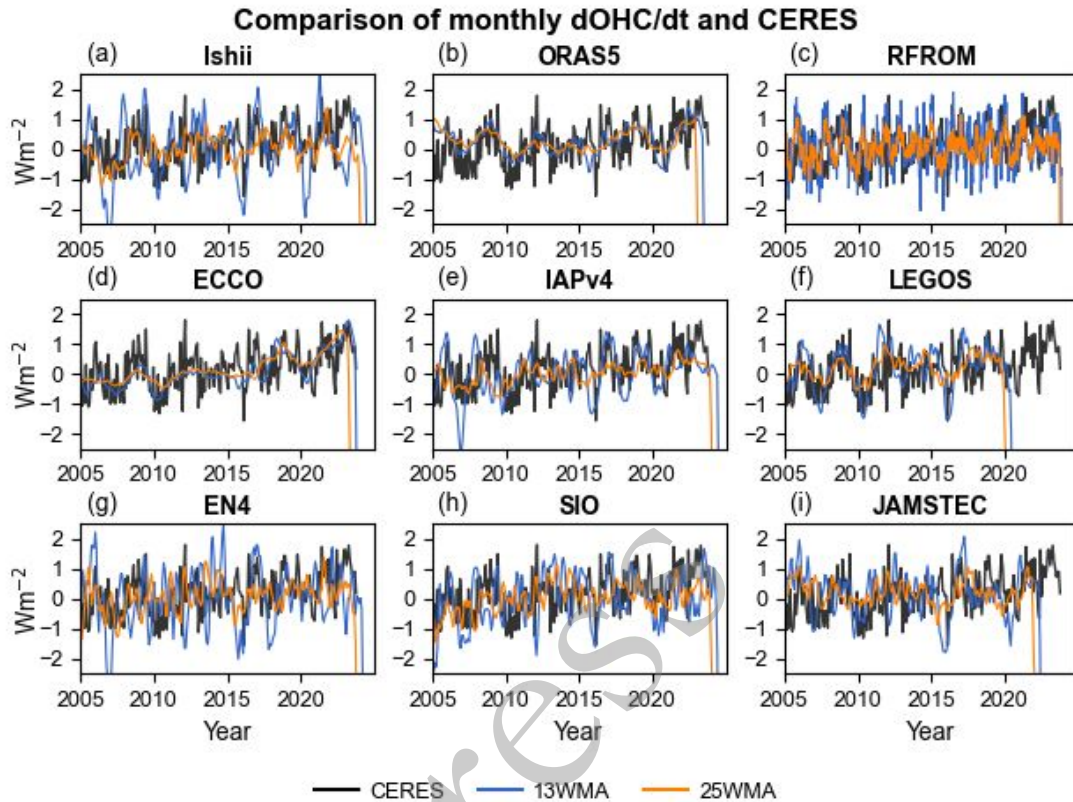
399

#### 400 ***3.4 Monthly Smoothing Sensitivity***

401 In addition to processing the annual average series, this study, following the  
402 approach of (Trenberth et al., 2016), directly applies smoothing to the original monthly  
403 OHC time series: a 13-month moving average (13WMA) and an extended 25-month  
404 moving average (25WMA) for further smoothing. Figure 5 displays the dOHC/dt time  
405 series after applying these two methods to all nine datasets. The figure visually indicates  
406 that the 13WMA method retains substantial amplitude. In contrast, the 25WMA method  
407 provides stronger smoothing, reducing the mean standard deviation of the dOHC/dt

408 series from  $1.72 \text{ W m}^{-2}$  (13WMA) to  $1.12 \text{ W m}^{-2}$ .

409



410

411 **Figure 5.** Impacts of different moving average windows on monthly dOHC/dt estimates,  
412 compared with monthly CERES-EEI. Each of the nine panels corresponds to a specific  
413 OHC dataset. Within each panel, the blue and orange lines represent the dOHC/dt time  
414 series calculated from the original monthly OHC data using a 13-month (13WMA) and  
415 a 25-month (25WMA) weighted moving average, respectively. The black line indicates  
416 the monthly CERES-EEI benchmark. All dOHC/dt series are calculated using central  
417 differencing.

418

419 In the comparison with CERES-EEI, the dOHC/dt series under both methods show

420 low coherence with the CERES-EEI series in terms of amplitude and temporal structure.

421 To quantify this observation, Figure 6 presents the correlation coefficients and RMSE

422 between dOHC/dt and CERES-EEI for the two methods. On average, across all nine

423 datasets, switching from 13WMA to 25WMA reduces the mean RMSE from 1.22 W

424  $m^{-2}$  to 0.98 W  $m^{-2}$ . However, the stronger smoothing conversely lowers the mean

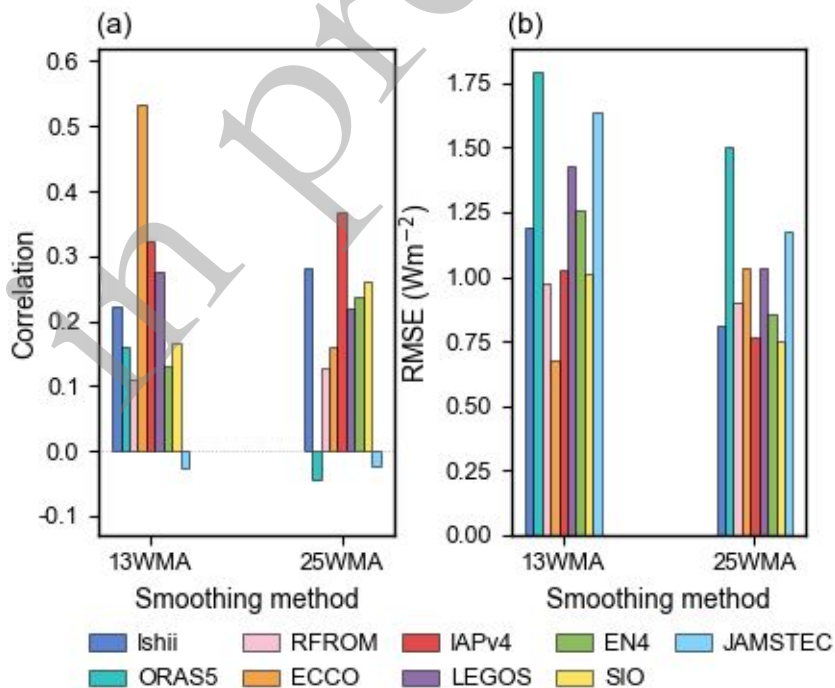
425 correlation coefficient from 0.21 (13WMA) to 0.18 (25WMA). This suggests that the

426 25-month smoothing window may excessively smooth some genuine interannual

427 signals, leading to reduced phase agreement with CERES. Overall, compared to the

428 dOHC/dt calculated directly from monthly data, the dOHC/dt derived from annual

429 processing demonstrates better consistency with CERES-EEI.



431

432 **Figure 6.** Quantitative comparison of monthly dOHC/dt estimates with monthly

433 CERES-EEI. a) the Pearson correlation coefficients and b) the Root Mean Square Error

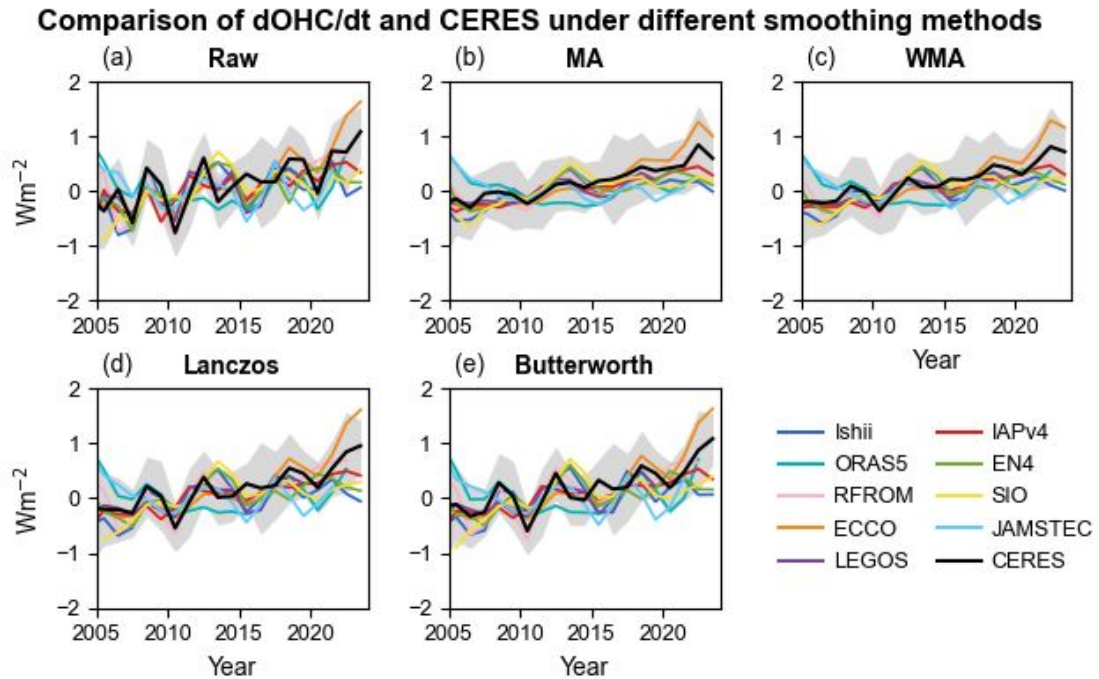
434 (RMSE) in  $W m^{-2}$ .

435

### 436 ***3.5 Data Sensitivity***

437 In addition to the time series processing methods discussed in previous sections,  
438 the OHC dataset itself is also a key source of uncertainty. This central finding is most  
439 clearly demonstrated in the line chart of Figure 7, which compares the  $dOHC/dt$  and  
440 CERES-EEI time series across different datasets under a fixed methodology. The  
441 amplitude variations differ among datasets across various time periods. Results show  
442 that for the RAW series subplot (Figure 7), the interannual amplitude (measured by  
443 standard deviation) of the datasets ranges from  $0.29 W m^{-2}$  to  $0.57 W m^{-2}$ . Furthermore,  
444 differences exist in the signal phase across datasets. In 2013, SIO and EN4 exhibit a  
445 phase opposite to that of ORAS5. For the estimation of the long-term trend, the  
446 uncertainty in trend introduced by the choice of dataset is  $0.29 W m^{-2} decade^{-1}$ ,  
447 constituting a relative uncertainty of approximately 83% relative to the overall mean  
448 trend ( $0.35 W m^{-2} decade^{-1}$ ). This indicates that the primary limiting factor for the  
449 accurate quantification of  $dOHC/dt$  is the dataset itself. The observed inter-dataset  
450 discrepancies are likely a composite of both random and systematic errors. These  
451 inconsistencies may stem from multiple factors, including differences in quality control  
452 (QC), bias correction, gap-filling techniques, and the CERES satellite instrument  
453 calibration errors.

454



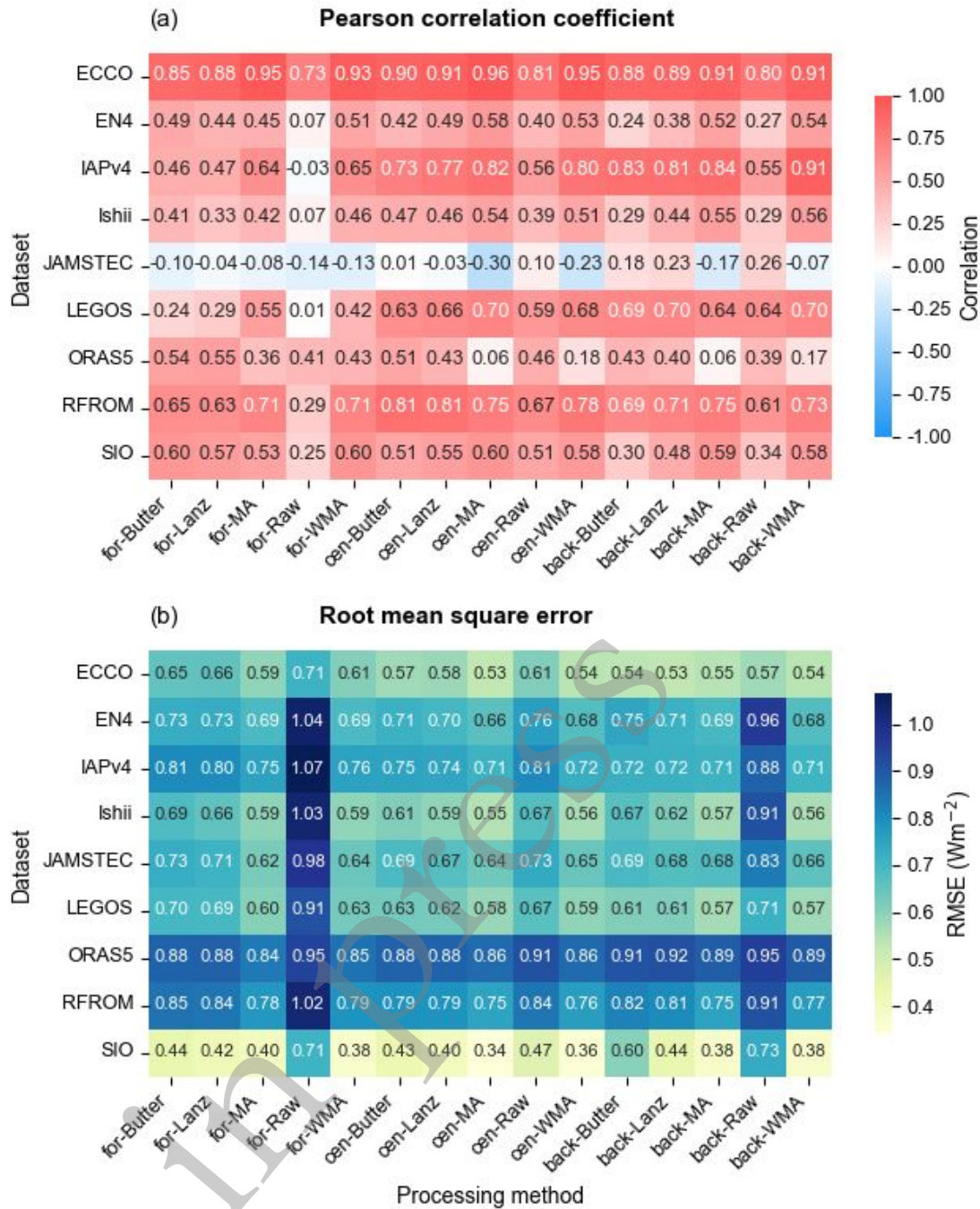
455

456 **Figure 7.** Inter-dataset comparison of central-differenced dOHC/dt estimates under  
 457 different smoothing methods, compared with CERES-EEI. Each of the five panels  
 458 corresponds to a specific smoothing method (including Raw). Within each panel,  
 459 colored lines represent the dOHC/dt time series from the nine different OHC datasets,  
 460 while the black line indicates the CERES-EE-I benchmark. The gray shaded area  
 461 represents the intra-annual  $\pm 1\sigma$  range of the CERES data. All dOHC/dt series are based  
 462 on the calendar-year (Jan-Dec) annual mean definition.

463

464 In the comparison with CERES-EEI, the amplitude and temporal structure of  
 465 dOHC/dt vary across different datasets. Figure 8 shows that, overall, OHC-based EEI  
 466 is consistent with CERES-EEI during certain periods (2007–2010). However, in other  
 467 periods, such as 2012–2015, SIO, EN4, and Ishii exhibit energy absorption maxima that  
 468 are completely opposite to the energy absorption minima of CERES-EEI, indicating

469 deviations. To quantify the differences among datasets, Figure 8 presents the RMSE  
470 and correlation coefficient results across all methodological combinations for the nine  
471 datasets. On average, for a given dataset, the fluctuation in RMSE (measured by  
472 standard deviation) due to changes in processing methods is  $0.10 \text{ W m}^{-2}$ . In contrast,  
473 for any given processing method, the fluctuation in RMSE due solely to switching  
474 between different datasets is  $0.15 \text{ W m}^{-2}$ . This indicates that, compared to time series  
475 processing methods, the primary source of inconsistency between current dOHC/dt  
476 estimates and CERES-EEI lies in the OHC datasets themselves. A further investigation  
477 into different types of datasets reveals that the internal spread among reanalysis datasets  
478 (RMSE of  $0.15 \text{ W m}^{-2}$ ) is higher than that of the objective analysis -based datasets  
479 (RMSE of  $0.12 \text{ W m}^{-2}$ ). A more comprehensive investigation on different types of data  
480 products are needed in the future.



481

482 **Figure 8.** Summary of performance metrics for dOHC/dt estimates across all datasets  
 483 and processing methods, compared with CERES-EEI. a) Heatmap of Pearson  
 484 correlation coefficients. b) Heatmap of RMSE values in  $W m^{-2}$ . In both panels, each  
 485 row corresponds to an OHC dataset, and each column represents one of the 15  
 486 combinations of differentiation and smoothing methods.

#### 488 **4. Conclusion and Discussion**

489 This study investigates the sensitivity of dOHC/dt estimates and their consistency  
490 with CERES-EEI to the choice of time series processing methods, including smoothing,  
491 differencing, and the definition of the annual mean. The results indicate that different  
492 processing methods represent a significant source of uncertainty in dOHC/dt estimation,  
493 though their influence is secondary to the inherent differences among OHC datasets  
494 themselves. Specifically, the choice of annual mean definition introduces a 14%  
495 (calculated as the standard deviation of the trend values,  $0.05 \text{ W m}^{-2} \text{ decade}^{-1}$ , divided  
496 by their absolute mean trend,  $0.35 \text{ W m}^{-2} \text{ decade}^{-1}$ ), relative uncertainty in the  
497 estimated long-term trend of dOHC/dt. Adopting the cross-year average definition  
498 removes some spurious interannual signals and improves the consistency between the  
499 raw ensemble mean dOHC/dt series and CERES-EEI. The choice of differencing  
500 method alters the phase and amplitude of the interannual signal in dOHC/dt and also  
501 introduces a 14% (calculated as the standard deviation of the trend values,  $0.04 \text{ W m}^{-2}$   
502  $\text{decade}^{-1}$ , divided by their absolute mean trend,  $0.29 \text{ W m}^{-2} \text{ decade}^{-1}$ ) relative trend  
503 uncertainty. The central difference method yields the strongest and most stable  
504 consistency between the calculated dOHC/dt and CERES-EEI. The choice of  
505 smoothing method has the smallest impact on the long-term trend of dOHC/dt (6%  
506 relative uncertainty) (calculated as the standard deviation of the trend values,  $0.02 \text{ W}$   
507  $\text{m}^{-2} \text{ decade}^{-1}$ , divided by their absolute mean trend,  $0.33 \text{ W m}^{-2} \text{ decade}^{-1}$ ), with its

508 primary role being the improvement of correlation with CERES. The selection of the  
509 OHC dataset is the absolute dominant factor in the current inconsistencies between  
510 dOHC/dt and CERES-EEI. The uncertainty in RMSE introduced by dataset choice  
511 (standard deviation:  $0.15 \text{ W m}^{-2}$ ) is greater than the typical uncertainty introduced by  
512 processing method choice ( $0.10 \text{ W m}^{-2}$ ). Furthermore, dataset selection introduces an  
513 83% (calculated as the standard deviation of the trend values,  $0.29 \text{ W m}^{-2} \text{ decade}^{-1}$ ,  
514 divided by the mean trend,  $0.35 \text{ W m}^{-2} \text{ decade}^{-1}$ ) relative uncertainty in the estimated  
515 long-term trend of dOHC/dt. Therefore, to further improve the accuracy of dOHC/dt  
516 estimation, future efforts must not only consider data processing procedures but, more  
517 critically, aim to reduce the systematic biases among different OHC datasets.

518 The findings of this study lead to several actionable recommendations for future  
519 research. To obtain more reliable dOHC/dt estimates, analyses should prioritize the use  
520 of the cross-year (Jul-Jun) annual mean and adopt the center difference method, which  
521 is demonstrably superior in phase accuracy and overall error. Furthermore, smoothing  
522 is critical for improving the intercomparison between dOHC/dt and CERES-EEI, robust  
523 filters (e.g., Lanczos, Butterworth) can be preferred.

524 This study primarily focuses on the uncertainty introduced by the choice of time  
525 series processing methods itself, but how these methods interact with the errors in the  
526 original data and data processing procedures, i.e., instrumental error and gap-infilling  
527 approach, is an equally important issue. All data-processing steps modulate the OHC  
528 estimate error. For example, the choice of annual mean definition, by altering the

529 combination of signals, can introduce or eliminate spurious errors (such as the peak  
530 during 2016-2017 in Section 3.1).

531 Differentiation, as a high-pass filter, can amplify high-frequency noise in the input  
532 data. However, the performance of different differencing schemes varies significantly.  
533 The analysis in Section 3.2 shows that the interannual standard deviation produced by  
534 central difference ( $0.27 \text{ W m}^{-2}$ ) is notably lower than that from forward ( $0.40 \text{ W m}^{-2}$ )  
535 and backward difference ( $0.43 \text{ W m}^{-2}$ ). Furthermore, smoothing methods, in turn, are  
536 intended to suppress errors by applying a low-pass filter, but this study's analysis  
537 reveals this to be an extremely complex trade-off process. On the one hand, smoothing  
538 significantly enhances the correlation with CERES. On the other hand, its contribution  
539 to reducing the overall absolute error (RMSE) is quite limited (an average reduction of  
540 only  $0.07 \text{ W m}^{-2}$ ). This result may suggest that the dominant residual error in the  
541 dOHC/dt series is not high-frequency random noise, but rather lower-frequency  
542 systematic issues in data and data processing (as revealed by inter-products differences).  
543 One illustrative example of this trade-off is that when the 3-year moving average (MA)  
544 is applied to the JAMSTEC dataset, its correlation coefficient deteriorates sharply to -  
545 0.30. This clearly demonstrates that a processing method aimed at suppressing  
546 uncertainty, if mismatched with the data's characteristics, can in fact severely distort  
547 the physical signal, thereby significantly amplifying the final estimation error.

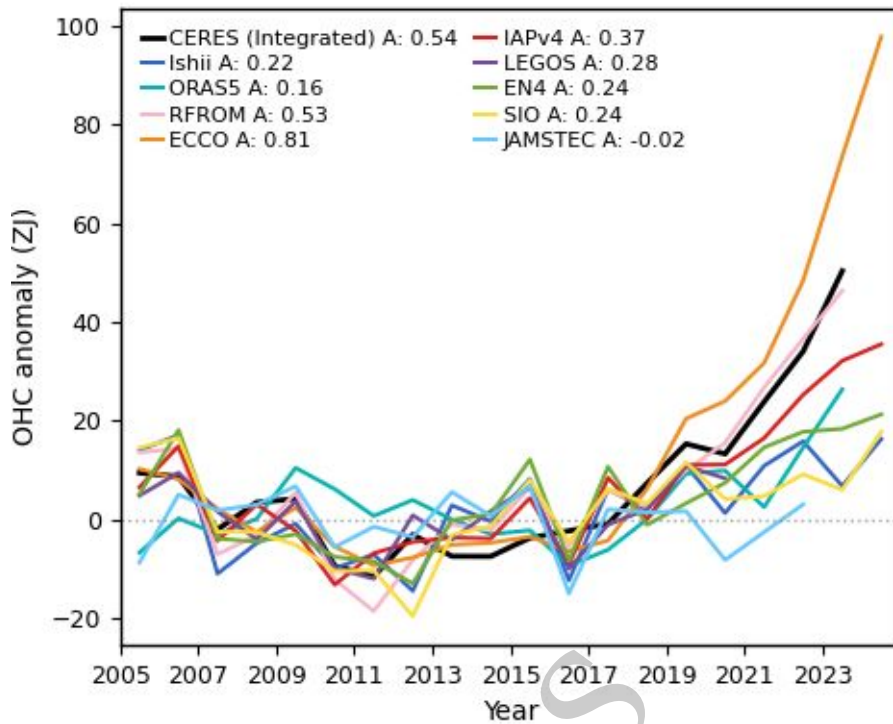
548 Beyond the general discussion on error propagation, specific findings from this  
549 study also highlight the close connection between physical processes and calculation

550 methods. The quantitative analysis in Section 3.2 shows that the backward difference  
551 method (mean  $r = 0.52$ ) systematically outperforms the forward difference method  
552 (mean  $r = 0.07$ ). This difference is intriguing, if not random, may have a physical  
553 explanation for instance the impacts of land/atmosphere heat storage and the ice melting  
554 energy, which might not be in phase with OHC changes. A deeper investigation into  
555 this physical mechanism presents a valuable direction for future research.

556       Considering that doing the time derivative can amplify errors, this study further  
557 explored whether integrating the EEI rather than differentiating it could yield better  
558 results (i.e. better consistency between OHC-EEI and CERES-EEI). Figure 9 compares  
559 the detrended OHC time series with the integrated CERES-EEI series. Before 2018, the  
560 interannual variations of most series were broadly similar; however, a systematic  
561 deviation occurred thereafter. The energy accumulation acceleration differs  
562 significantly across datasets, ranging from  $-0.02$  to  $+0.81 \text{ W m}^{-2} \text{ decade}^{-1}$ . To further  
563 evaluate whether the integration method outperforms differencing, this study compares  
564 the uncertainty in acceleration estimates between the two approaches. The trend  
565 uncertainty among datasets (measured by standard deviation) obtained using the  
566 integration method is  $0.24 \text{ W m}^{-2} \text{ decade}^{-1}$ , representing a reduction of approximately  
567 17% from the  $0.29 \text{ W m}^{-2} \text{ decade}^{-1}$  uncertainty of the differencing method.  $\text{W m}^{-2}$   
568  $\text{decade}^{-1}$   $\text{W m}^{-2} \text{ decade}^{-1}$  This indicates that the integration method reduces errors by  
569 effectively suppressing noise.

570

### Detrended OHC and CERES integrated comparison



571

572 **Figure 9.** Comparison of detrended OHC anomalies from nine datasets with the  
573 integrated CERES-EEI. The colored curves represent detrended OHC anomalies (in ZJ)  
574 for different OHC datasets, while the solid black line shows the detrended time-  
575 integrated CERES radiative flux anomalies. Results based on the Jan-Dec mean. The  
576 legend value 'A' for each series is the ocean warming acceleration (in W m<sup>-2</sup> decade<sup>-1</sup>),  
577 derived from a quadratic fit to the original (non-detrended) time series.

578

579 The findings of this study indicate that when comparing different OHC-based EEI  
580 estimates with CERES-EEI, it is essential to fully account for the differences introduced  
581 by data processing methods, such as smoothing, differencing, and the definition of the  
582 annual mean. Future efforts should focus on optimizing observation systems,  
583 standardizing data processing protocols, and enhancing multi-source data assimilation

584 to reduce uncertainties and improve the accuracy of dOHC/dt estimates. Addressing  
585 these issues will not only enable a more precise quantification of the Earth's energy  
586 budget but also provide more reliable observational constraints to help evaluate climate  
587 models and reduce uncertainties in their estimates of future climate.

588

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597 the national programmes contributing to it (<https://argo.ucsd.edu>, [https://www.ocean-](https://www.ocean-ops.org)  
598 [ops.org](https://www.ocean-ops.org)). The Argo Program is part of the Global Ocean Observing System. We are  
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601 used in this study.

602 ***Data availability statement.*** The datasets utilized in this study are publicly  
603 available from the following sources. The IAPv4 dataset can be accessed via  
604 <http://www.ocean.iap.ac.cn/pages/dataService/dataService.html?>. The Ishii dataset is

605 available at <https://climate.mri-jma.go.jp/pub/ocean/ts/v7.3.1/>, and the EN4 dataset can  
606 be obtained from <https://www.metoffice.gov.uk/hadobs/en4/index.html>. The SIO  
607 dataset is accessible at [https://sio-argo.ucsd.edu/RG\\_Climatology.html](https://sio-argo.ucsd.edu/RG_Climatology.html), while the  
608 JAMSTEC dataset is available from  
609 [https://www.jamstec.go.jp/argo\\_research/dataset/moaagpv/moaa\\_en.html](https://www.jamstec.go.jp/argo_research/dataset/moaagpv/moaa_en.html). For  
610 reanalysis data, the ECCO dataset can be retrieved from <https://ecco-group.org/ohc.htm>,  
611 and the ORAS5 dataset is available at  
612 <https://www.ecmwf.int/en/forecasts/dataset/ocean-reanalysis-system-5>. Among  
613 satellite-based data, the LEGOS dataset is accessible via  
614 <https://earthobservation.magellium.com/project/moheacan/?lang=en>, and the CERES  
615 dataset can be obtained from <https://ceres.larc.nasa.gov/data/>. The fused data PMEL  
616 RFROM is available at <https://www.pmel.noaa.gov/rfrom>.

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